

# Applications of Ehrenfest dynamics: from excited state evolution of protected gold clusters to stopping of high-energy ions in graphene

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# Background

- Shift of interest from ground state electronic structure calculations towards processes and phenomena
- Many processes, such as ion-atom collisions or electron transfer in biomolecules, are nonadiabatic
  - The process is not dictated by a single electronic state, but instead by two or more coupled states
- Ehrenfest dynamics (ED) + time-dependent DFT + PAW = a computationally affordable framework for studying nonadiabatic processes

# Ehrenfest dynamics in GPAW

- Conservation of the total energy leads to Ehrenfest dynamics equations within the PAW method<sup>1</sup>

$$\text{electrons } i\tilde{S}\frac{\partial\tilde{\psi}_n}{\partial t} = (\tilde{H} + \tilde{P})\tilde{\psi}_n = (\tilde{H} - i\sum_a \dot{\mathbf{R}}_a \cdot \hat{\mathbf{D}}_a)\tilde{\psi}_n$$

$$\text{nuclei } M\ddot{\mathbf{R}}_a = -\nabla_{\mathbf{R}_a} E_{\text{KS}} + \sum_n f_n \langle \tilde{\psi}_n | \hat{\mathbf{D}}_a^\dagger \tilde{S}^{-1} \tilde{H} + c.c. | \tilde{\psi}_n \rangle$$

$\tilde{P}$  term accounts for the position-dependent augmentation operator, with

$$\hat{\mathbf{D}}_a = \mathcal{T}^\dagger \frac{\partial \mathcal{T}}{\partial \mathbf{R}_a} = (1 + \hat{t}_a^\dagger) \frac{\partial \hat{t}_a}{\partial \mathbf{R}_a} \quad \text{and} \quad \hat{t}_a = \sum_i (|\phi_i^a\rangle - |\tilde{\phi}_i^a\rangle) \langle \tilde{p}_i^a|$$

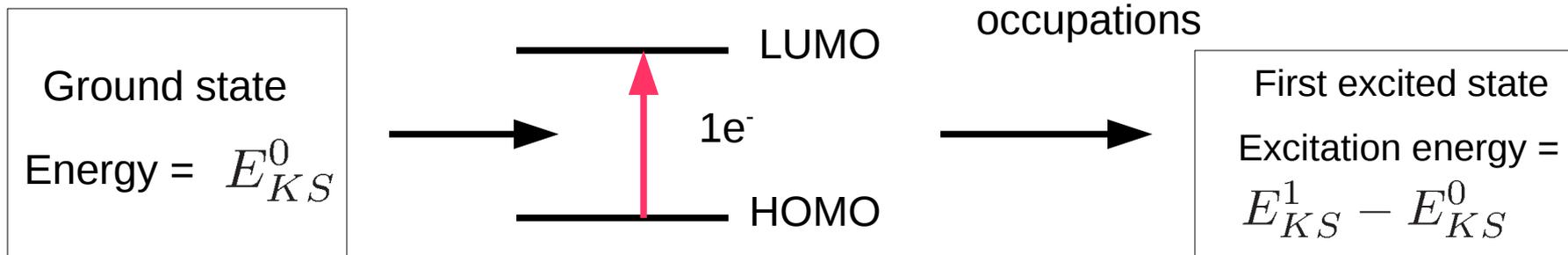
- In practice, simultaneous solution using
  - Time propagator (SICN) for the electrons
  - Velocity Verlet for the nuclei

# Excited state evolution of a protected gold cluster

- Protected metal nanoparticles = a novel class of luminescent nanomaterials
  - Applications: medicine, imaging and catalysis
- Exact mechanism at the origin of the luminescence of gold clusters is not understood
  - Better knowledge of the interaction between the gold core and the surrounding ligands, and the photo-induced dynamics required!
- We investigated<sup>1</sup> the photo-induced dynamics of a protected Au<sub>2</sub> cluster using Ehrenfest dynamics in conjunction with the Delta Self-Consistent-Field method

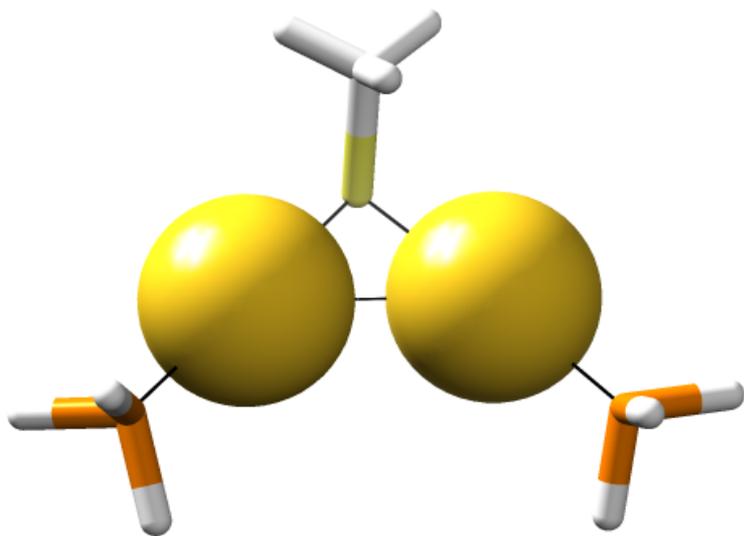
# The Delta-SCF+Ehrenfest method

## Delta Self-Consistent Field



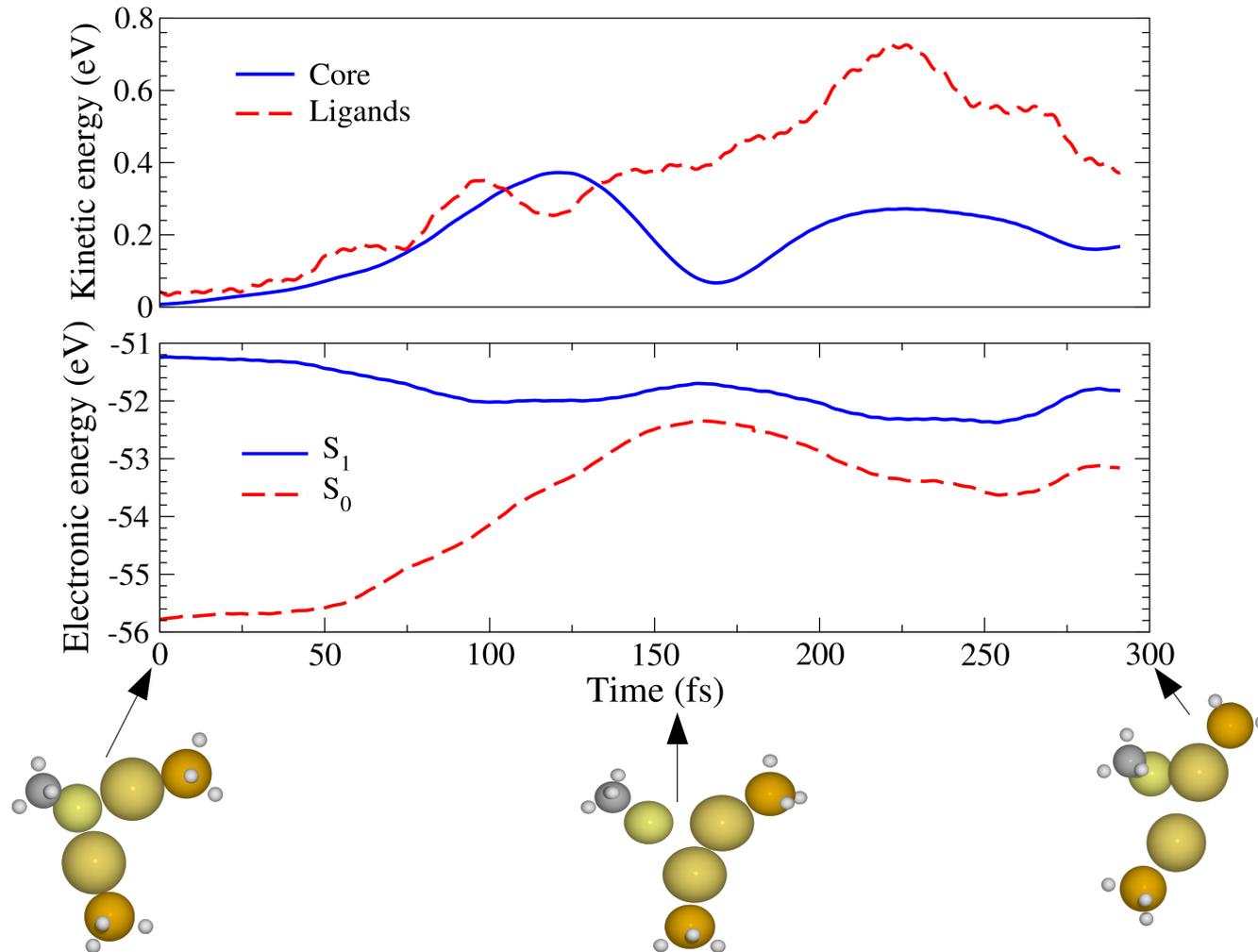
- Excitation energies from spin-unpolarized Delta-SCF often very close to linear-response TDDFT
- Initial state with Delta-SCF, photoexcitation dynamics from Ehrenfest dynamics

# Simulation details



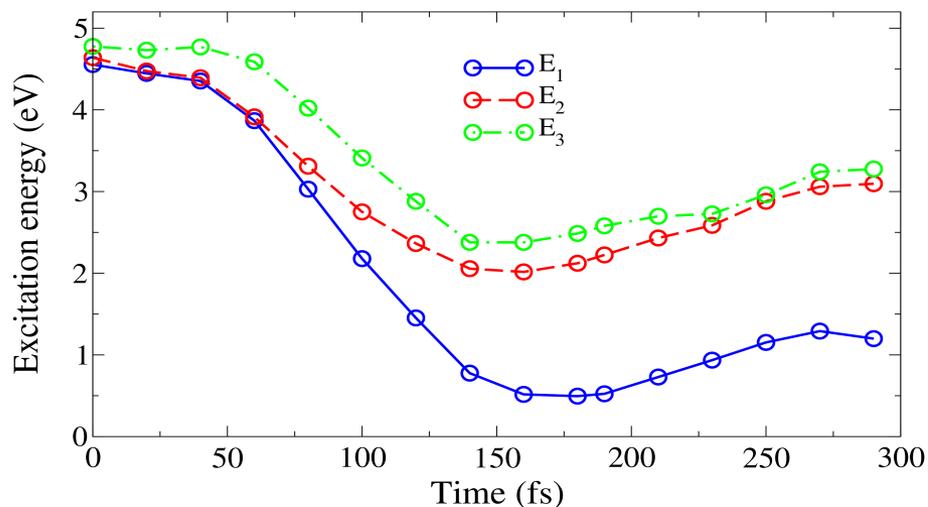
- Au<sub>2</sub> cluster protected by one SCH<sub>3</sub> and two PH<sub>3</sub> groups
- 300 fs long calculations with a small initial kinetic energy
- Grid spacing  $h = 0.2 \text{ \AA}$ ,  $5 \text{ \AA}$  vacuum around the ligands, PBE XC functional

# Evolution of the nuclei and electrons

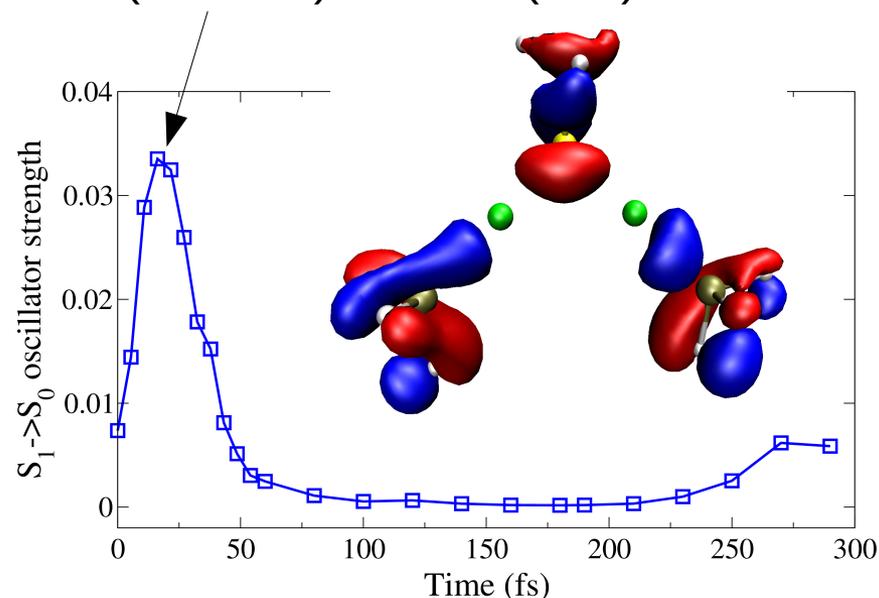


# Linear-response TDDFT results

- for the trajectory obtained with Ehrenfest dynamics

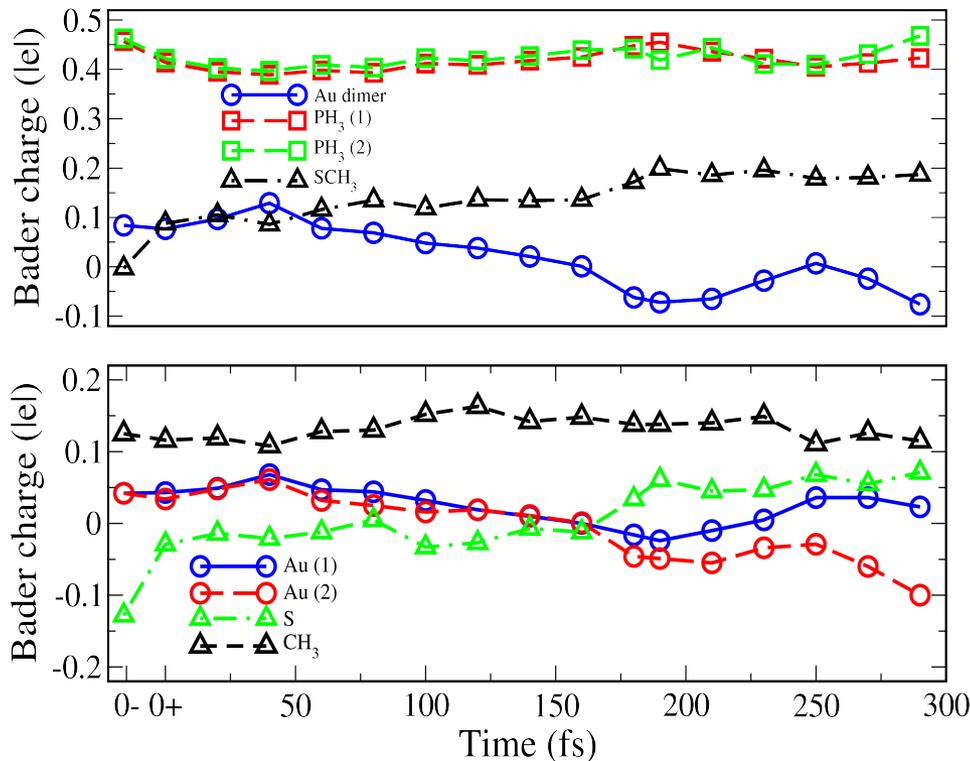


LUMO( $t = 25$  fs) – LUMO( $t = 0$ )



Increased oscillator strength at the beginning and at the end of the simulation

# Charge transfer analysis



- Excitation ( $0^- \rightarrow 0^+$ ) localized in the ligands
- Metal-to-ligand charge transfer (first 50 fs), ligand-to-metal thereafter
- Asymmetric charge distribution in the gold core at the end

# Au<sub>2</sub> cluster: conclusions

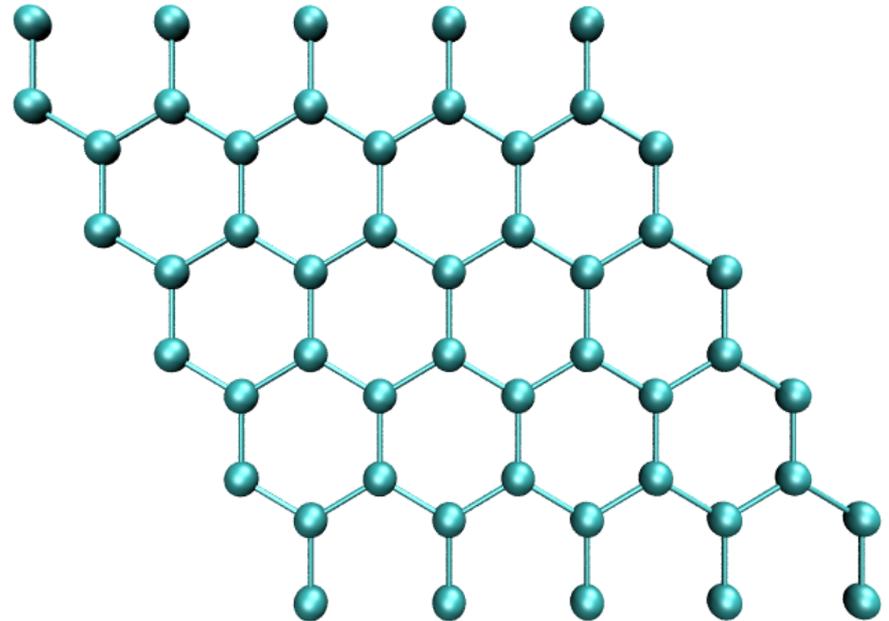
- Complex dynamics in spite of the simple core
- Metal-to-ligand charge transfer during first 50 fs, reversed thereafter
  - Increased oscillator strength coupled to accumulation of charge around the P atoms, suggesting use of stronger electron-accepting groups in the phosphine ligands to enhance emission
- Asymmetric charge distribution in the core at the end
  - Coupled to increased oscillator strength
  - This mechanism might be present in the excited state dynamics of larger protected cluster

# Stopping of high-energy ions in graphene

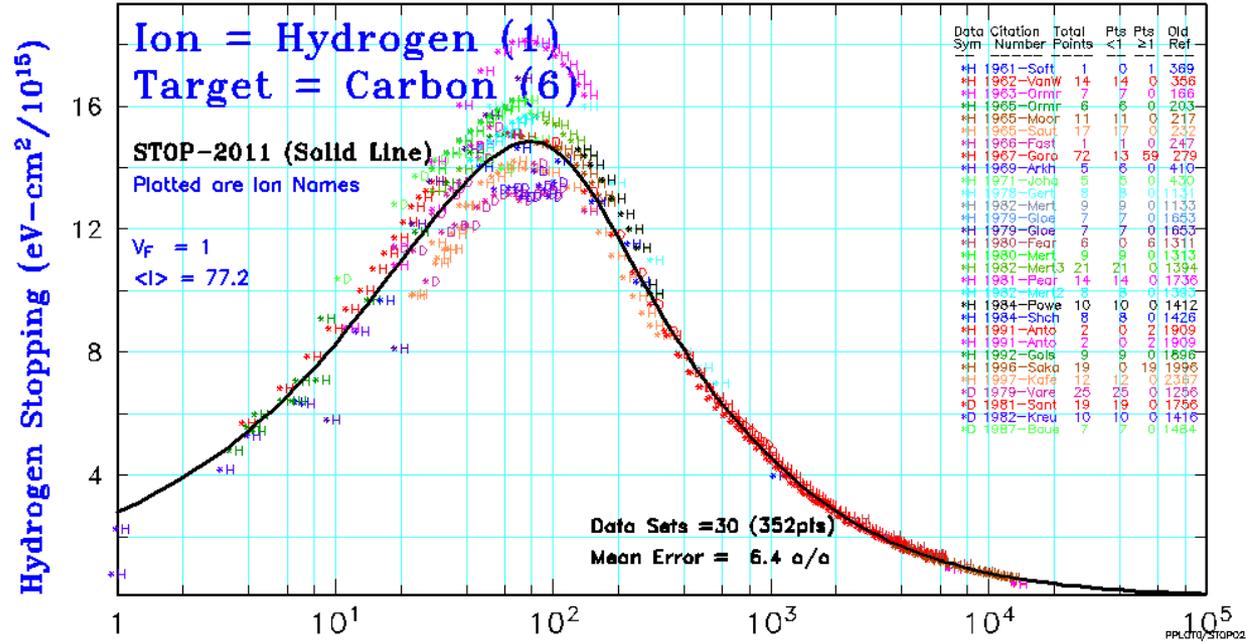
- In ion bombardment, the projectile loses kinetic energy to
  - collisions with the nuclei (nuclear stopping)
  - electronic excitations in the target or in the projectile (electronic stopping)
- Ab initio description of electronic stopping difficult
  - Especially at high impact energies, at which core electron excitations start to contribute to the stopping process
- By bombarding graphene with high-energy ions, we studied<sup>1</sup> the capability of Ehrenfest dynamics for modeling electronic stopping from first principles

# Simulation details

- Main quantity of interest: energy deposited into the electrons of the target and the projectile
  - Can be converted into stopping power  $S_e$  if the thickness of the target is known
- Slabs composed of up to 6 layers of graphene, 50 atoms in each layer
- Periodic boundary conditions in all directions, singly ionized projectiles
- Spacing  $h = 0.2 \text{ \AA}$ , LDA XC



# Electronic stopping: experiments

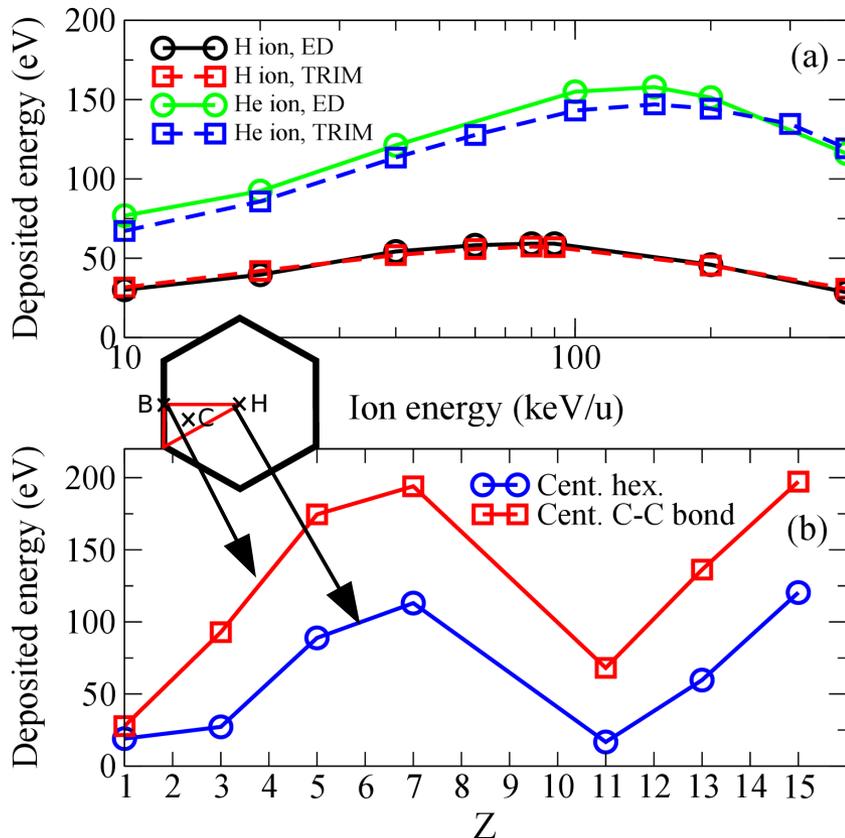


'Experiments' = best fit to a large amount of experimental data for carbon, obtained from the semi-empirical code TRIM (black line)

In order to do the comparison, we calculate the average stopping over the graphene surface (requires several trajectories / energy)

# Stopping of light ions

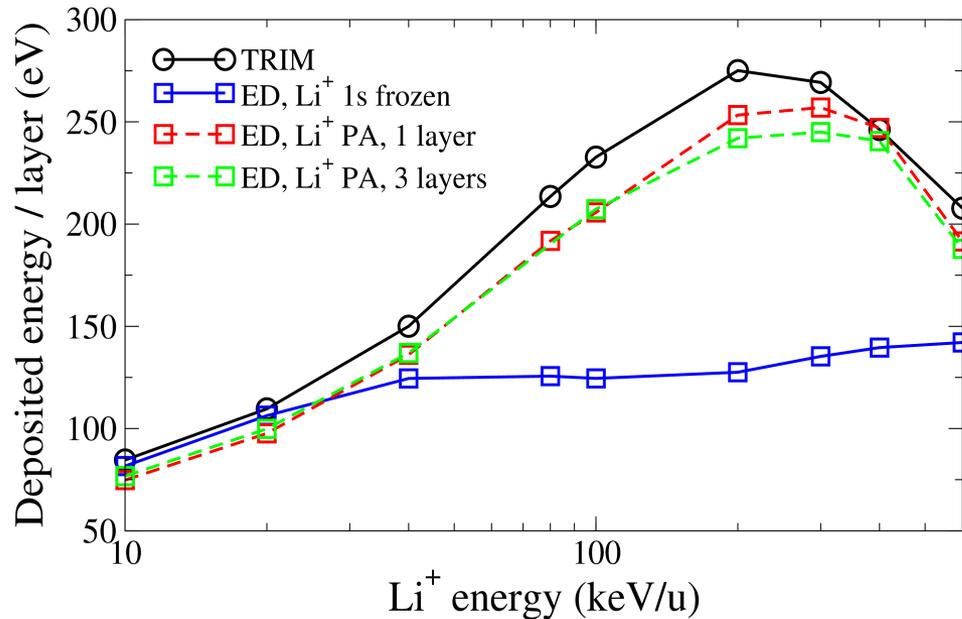
Top figure: ED results represent an estimated average over the graphene surface



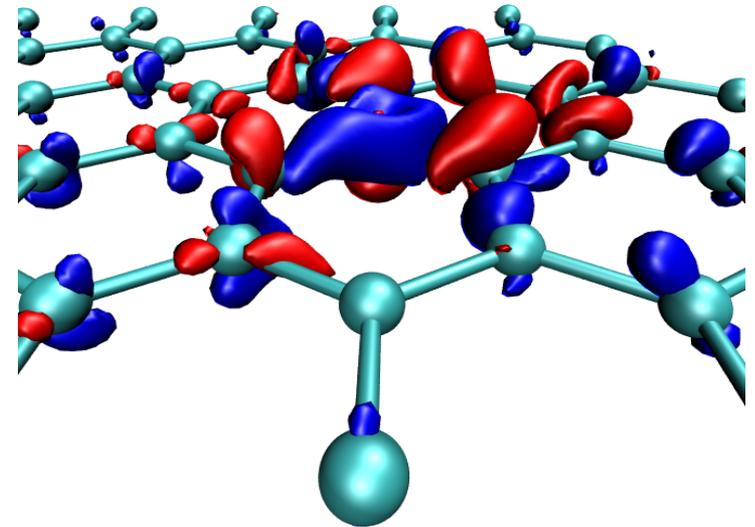
- Good agreement between ED results and experiments (TRIM) for H and He ions
- Stopping power oscillates as a function of nuclear charge Z, in agreement with earlier experimental observations

# High-energy stopping for Li

Li “pseudoatom” (PA): core electrons treated as valence electrons within the PAW scheme



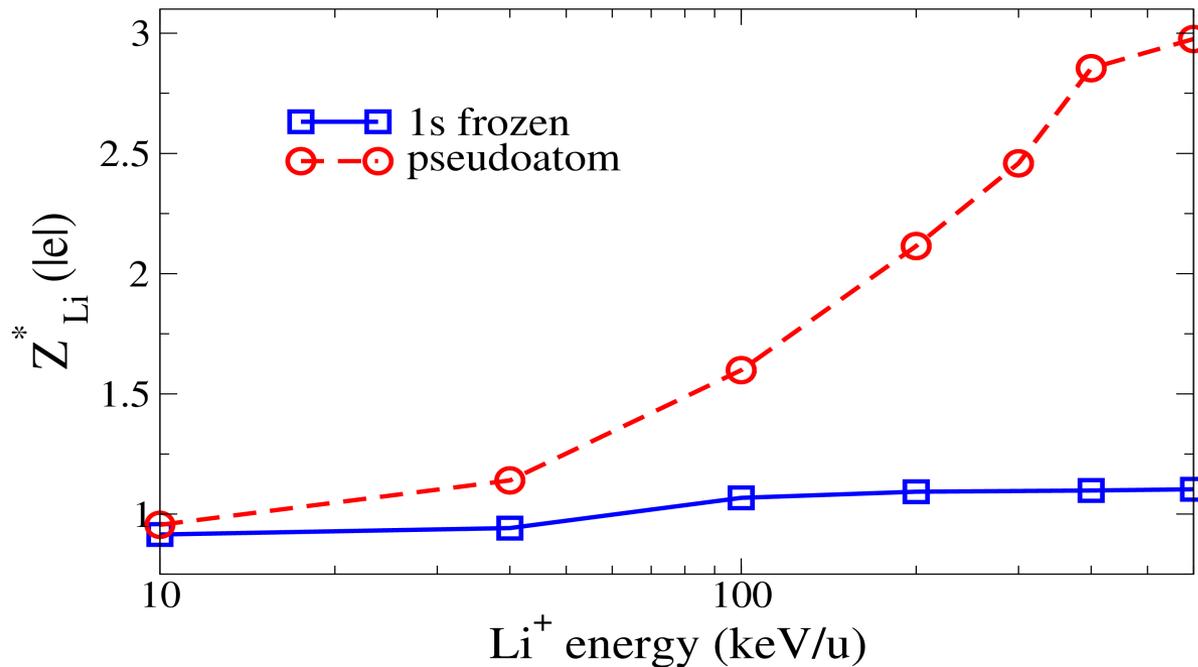
200 keV/u: difference between densities obtained using PA-Li and Li with 1s frozen



Huge improvement at high energies with the 3-electron setups!

# Li stopping: ionization

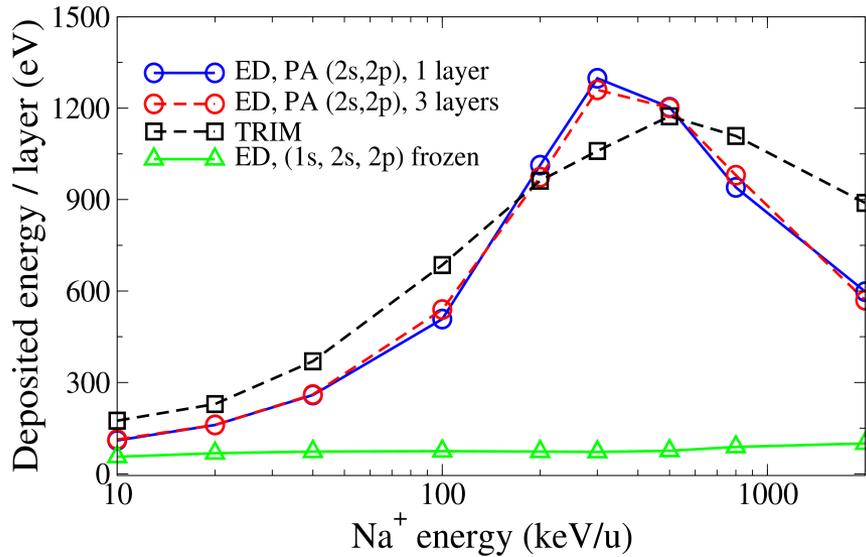
- $Z^*$  = integrated all-electron density around the projectile just after passing through the target



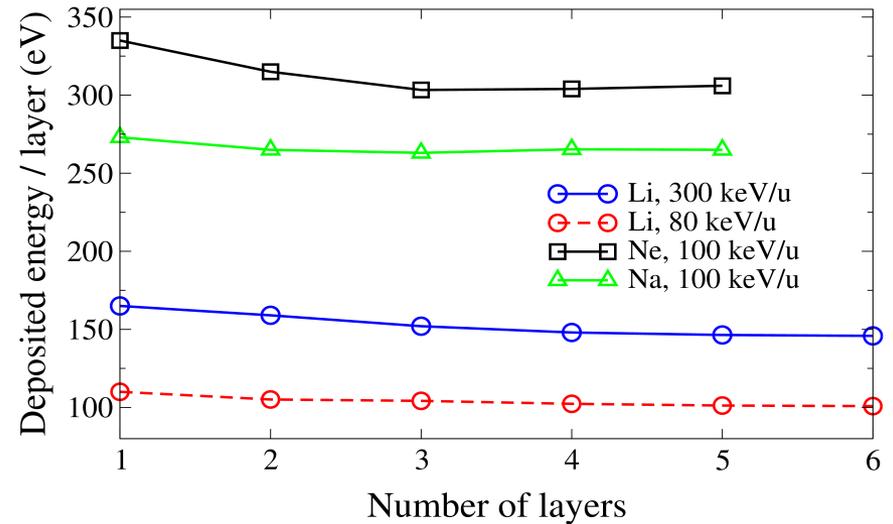
Increase in projectile charge coupled to increase in stopping power!

# Results for sodium projectile and multiple graphene layers

## Na (2s, 2p included) vs frozen-core



## Li, Na as before, Ne (1s frozen)



# High-energy stopping: conclusions

- Ehrenfest dynamics provides a quantitatively accurate description of electronic stopping for light projectiles
- Decent agreement between ED+pseudoatom results and experiments for higher-mass projectiles at high energies
  - Excellent result since core electron excitations are generally difficult to model!
- Our computational setup can also be used for simulating the impact of ions with a high charge state
  - The projectile can be ionized in the collision with an intermediate target

# Thank you!

...and big thanks to CSC and the Triton cluster of the Aalto University for the computational resources!



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