

Computational Screening of Materials for Water Splitting

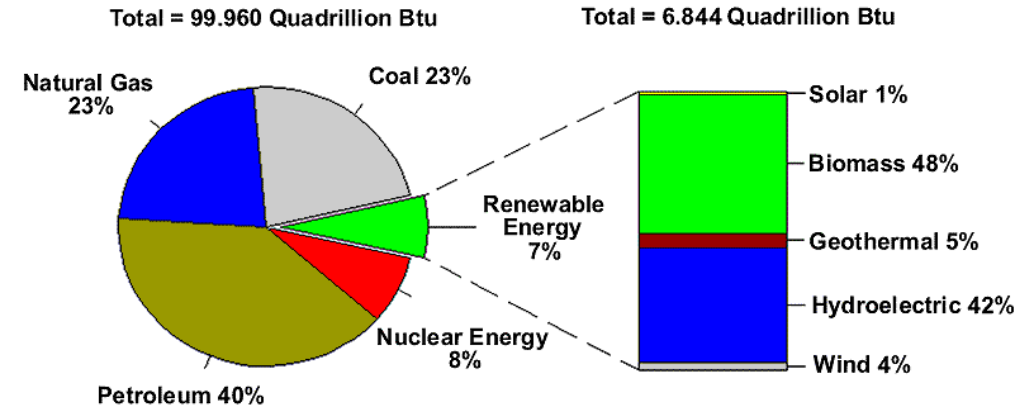
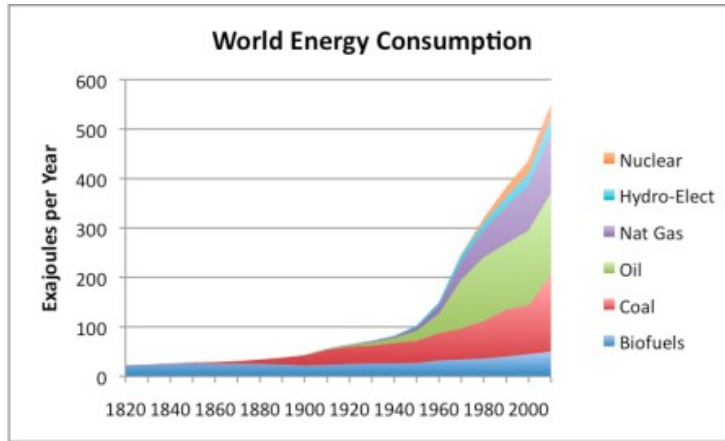
I.E. Castelli, K.S. Thygesen, and K.W. Jacobsen

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Department of Physics
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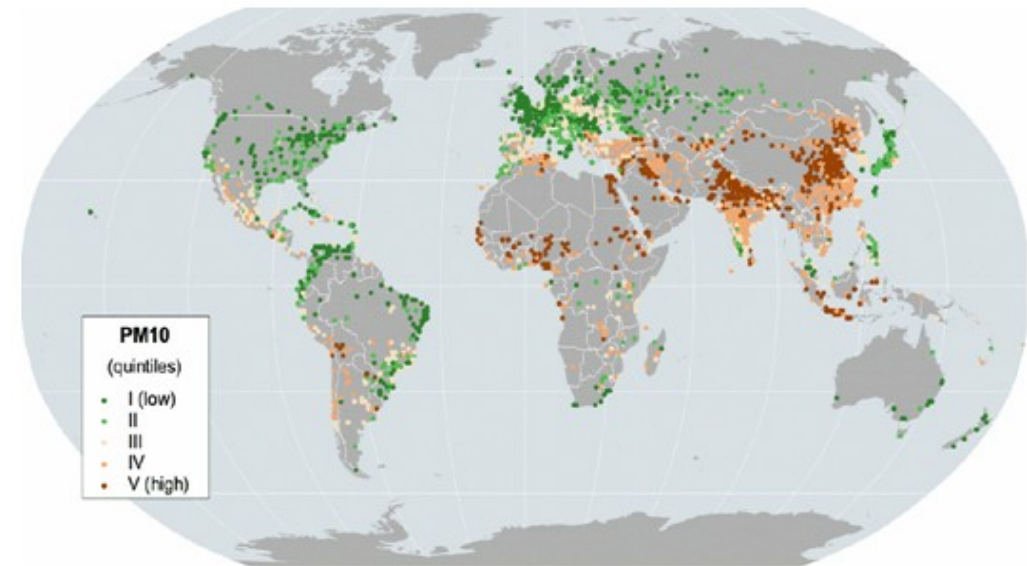
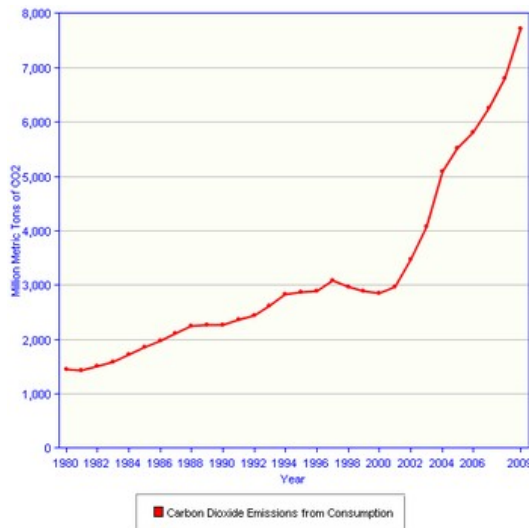
GPAW Workshop
22 May 2013

The World Needs Clean Energy

More/cheap
energy



Less pollutants
(CO₂, NO_x, PM10)

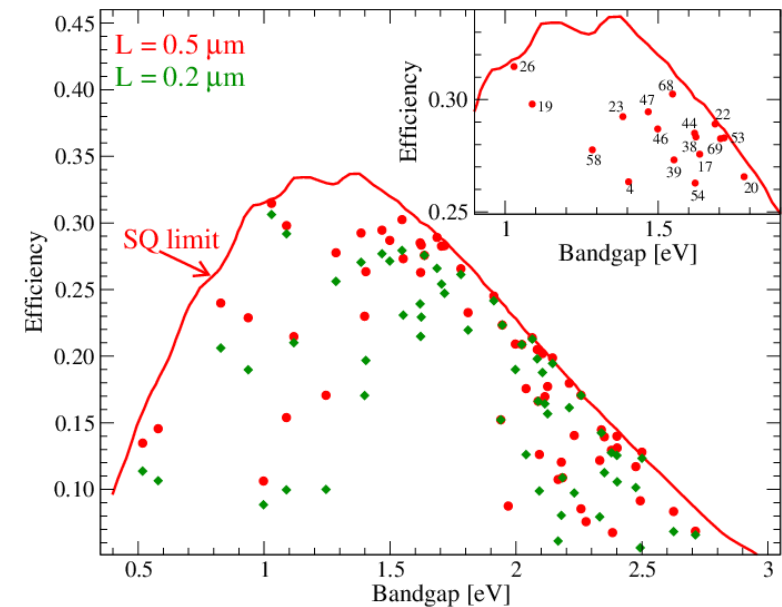
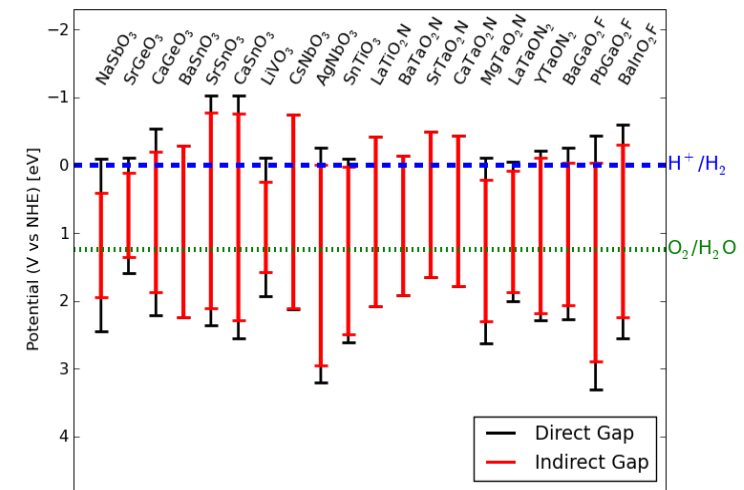


Conclusions

Few materials (40) identified for one- and two-photon water splitting;

The GLLB-SC potential works well for bandgap calculations;

17 materials proposed for single-layer thin film solar cell.



Photoelectrochemical Cell

Computational search for materials able to collect the visible part of the solar spectrum and to split water in oxygen and hydrogen.

Complicated process:

- Light absorption;
- Electron-hole mobility;
- Induce reactions.



Few examples: TiO_2 , GaN:ZnO , $\text{ZnGeN}_2:\text{ZnO}$

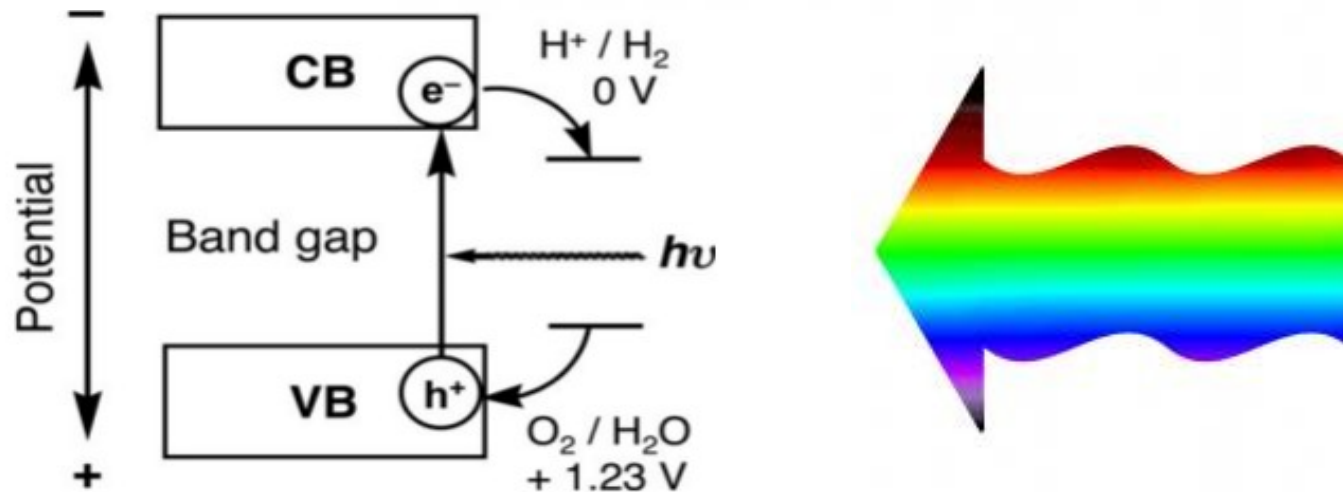
Fujishima and Honda, *Nature* **238**, 37 (1972).

Maeda *et al.*, *JACS* **127**, 8286 (2005).



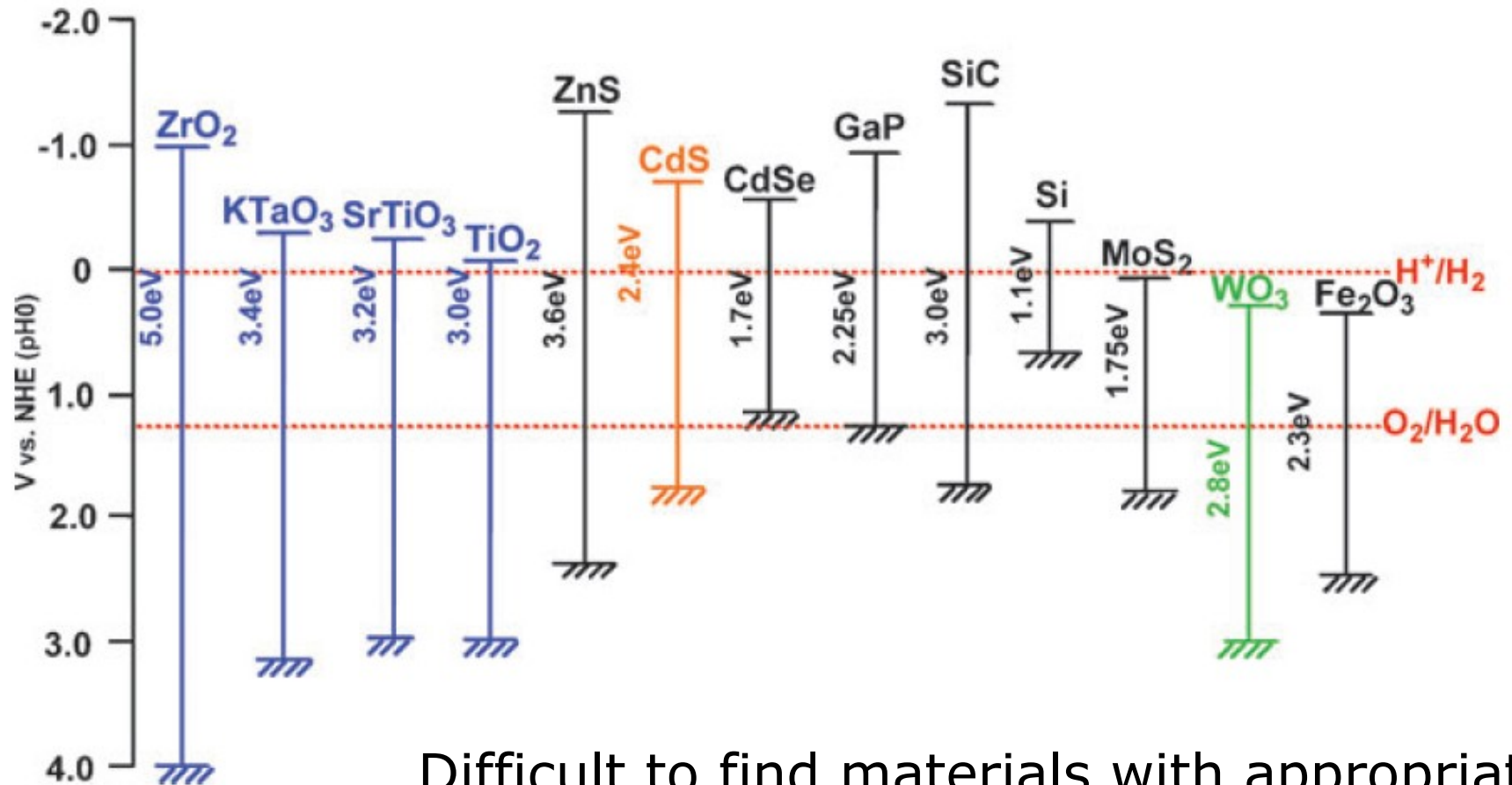
Materials for Water Splitting

- 1) **Chemical/structural stability;**
- 2) **Bandgap in the visible range (1.5 - 3 eV);**
- 3) **Band edge positions straddle the water red-ox potentials;**
- 4) Good electron/hole mobility;
- 5) Good catalytic properties;
- 6) Low cost and non-toxicity.



Principle of water splitting using semiconductor photocatalysts.

Possible Solutions



Difficult to find materials with appropriate bandgap and band edge positions!

Kudo and Miseki, *Chem. Soc. Rev.* **38**, 253 (2009).



1) Stability Analysis

Perovskite compared with a pool of reference systems (400 compounds, from the ICSD experimental database):

- Single metal bulk: $A(s)$ and $B(s)$;
- Single metal oxides (nitrides, ...): $A_xO_y(s)$;
- Bi-metal oxides (nitrides, ...): $A_xB_yO_z(s)$;
- Single and bi-metal oxinitrides (oxyfluorides, ...): $A_xO_yN_z(s)$ and $A_xB_yO_zN_k(s)$.

Energies calculated from DFT: RPBE xc-functional.

Formation energy (solved by linear programming):

$$\Delta E = ABO_3(s) - \min_{c_i} (c_1A(s) + c_2B(s) + c_3A_xO_y(s) + c_4B_xO_y(s) + c_5O)$$
$$c_1 + c_3 = 1, \quad c_2 + c_4 = 1, \quad c_3 + c_4 + c_5 = 3$$



2) Calculation of the bandgaps: GLLB-SC

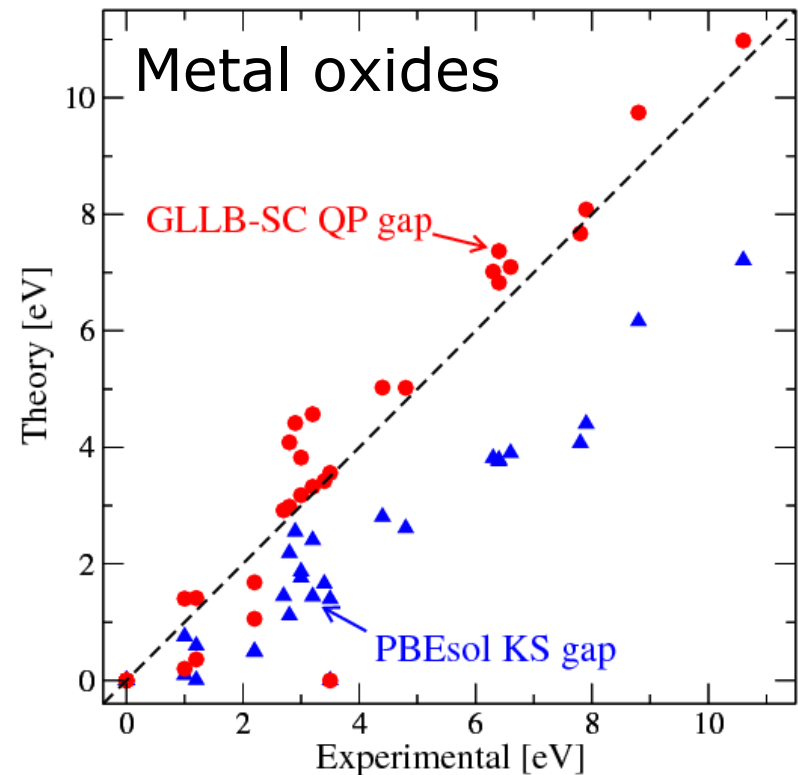
First description: Gritsenko *et al.*, *Phys. Rev. A* **51**, 1944 (1995).

Implemented in GPAW: Kuisma *et al.*, *Phys. Rev. B* **82**, 115106 (2010).

$$E_g^{QP} = E_g^{KS} + \Delta_{xc}$$

Minimal computational cost.

Gap within an error 0.5 eV.



I. E. Castelli, T. Olsen, S. Datta, D. D. Landis, S. Dahl, K. S. Thygesen, and K. W. Jacobsen, *Energy & Environmental Science*, **5**, 5814 (2012).

3) Evaluation of the band edges

Empirical formula: $E_C = (\chi_A \chi_B \chi_O^3)^{1/5} - 1/2 E_{gap} + E_0$

$$\chi = 1/2 (A + I_1)$$

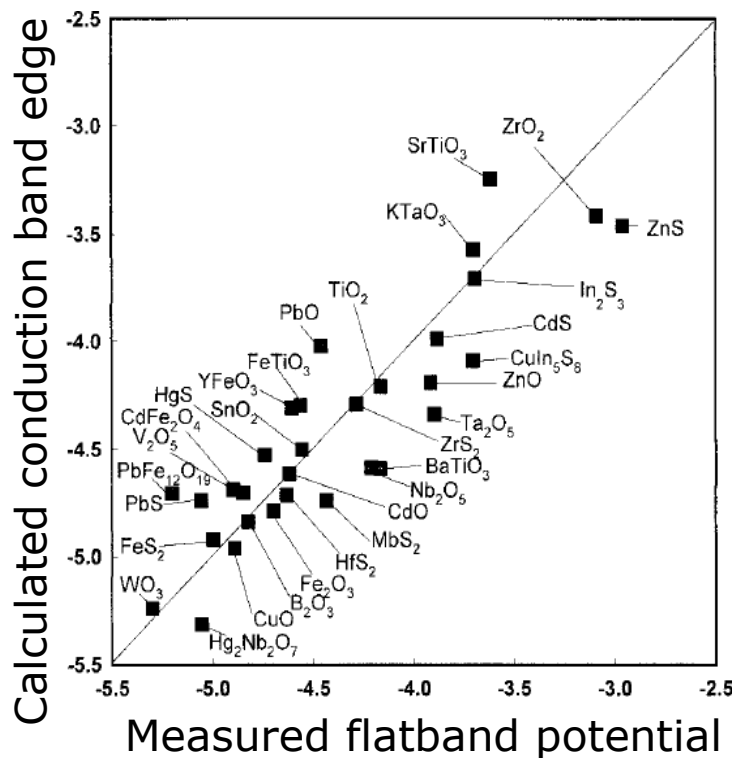
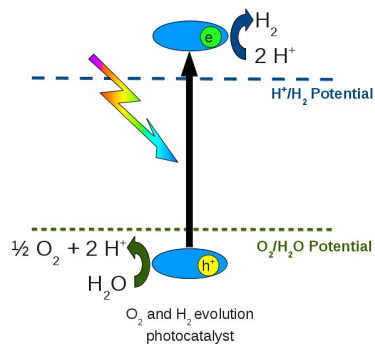
= Absolute electronegativity (Mulliken scale).

A = electron affinity

I_1 = first ionization energy

E_{gap} = Bandgap.

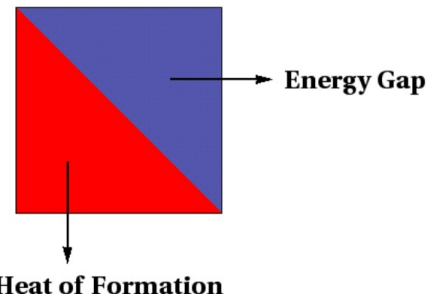
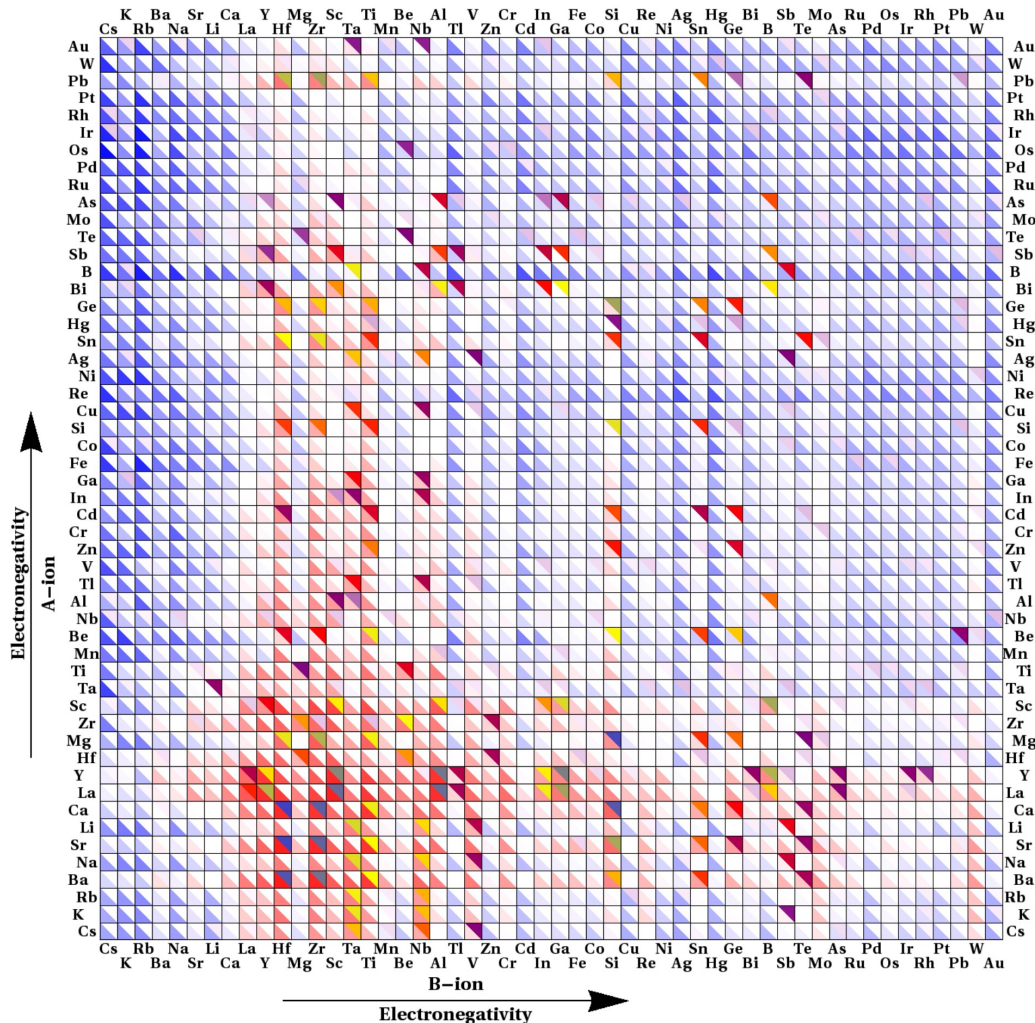
E_0 = Reference electrode redox level to the vacuum.



Butler and Ginley, *J. Electrochem. Soc.* **125**, 228 (1978).

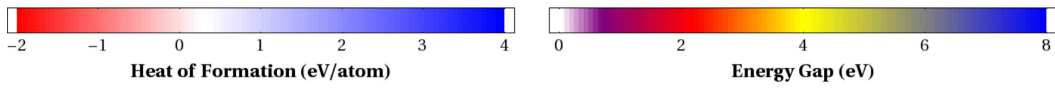
Xu and Schoonen, *Am. Mineral.* **85**, 543 (2000).

ABO₃ Perovskite

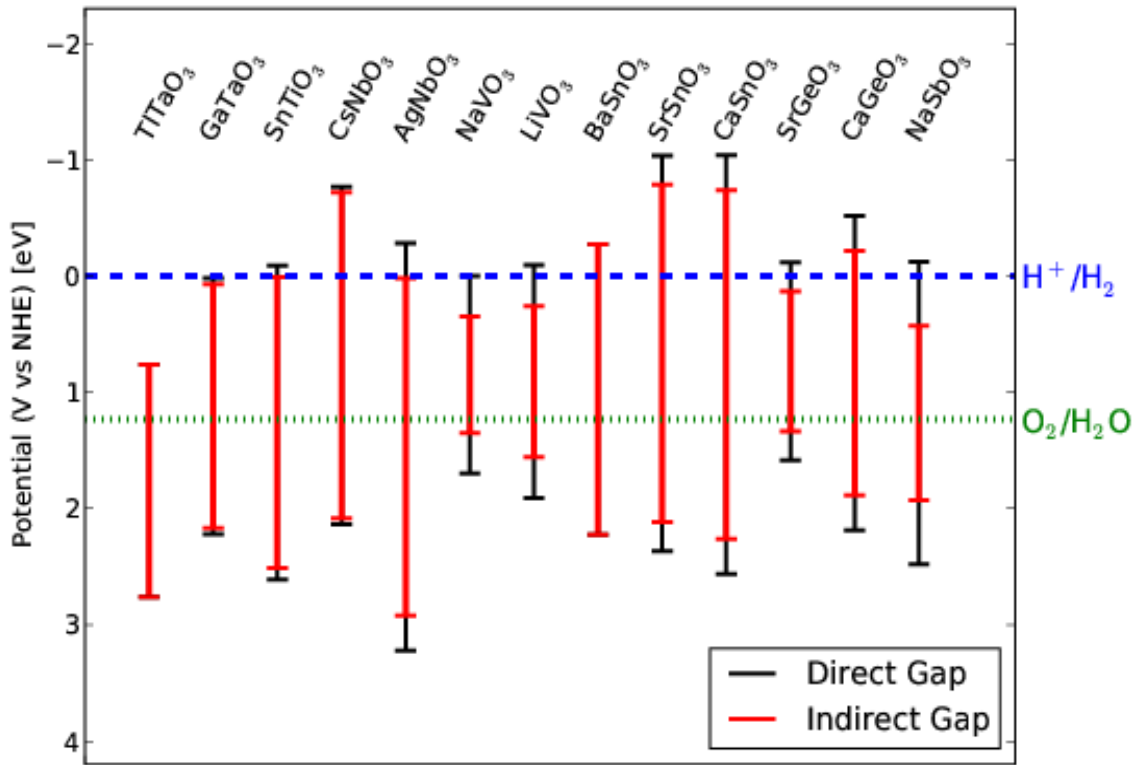


Chemical-based rules for stability and bandgap:

- Goldsmith's tolerance factor;
- even number of electrons in the unit cell;
- sum of the possible oxidation states = 6.



Candidates for One-photon WS - Oxides



AgNbO₃ and BaSnO₃ are known:

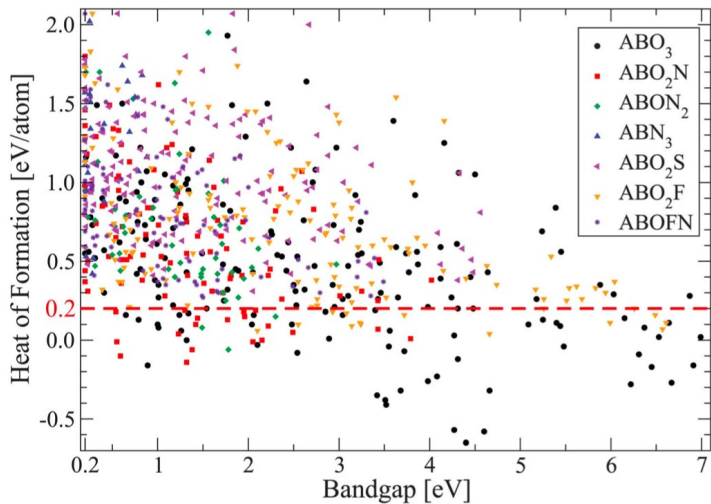
AgNbO₃: works!

BaSnO₃: defect induced recombination.

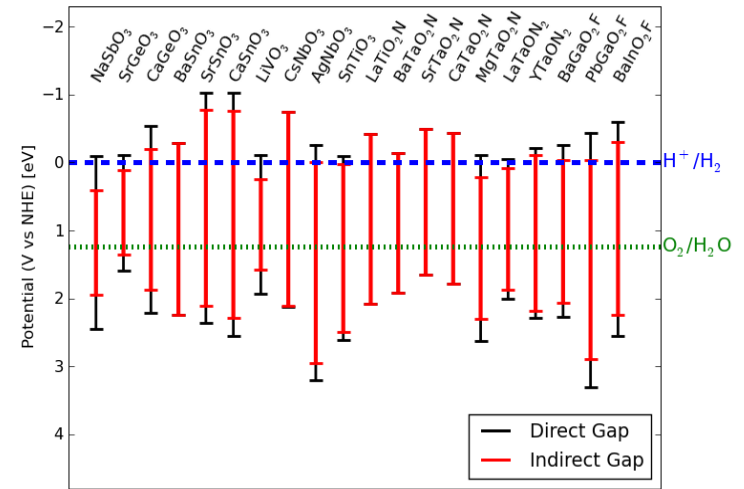
SrSnO₃ and CaSnO₃: orthorhombic perovskite (too large bandgap).

None of the others is known.

Candidates for One-photon WS



~19000 materials



20 candidates

Screening parameters

One-photon WS

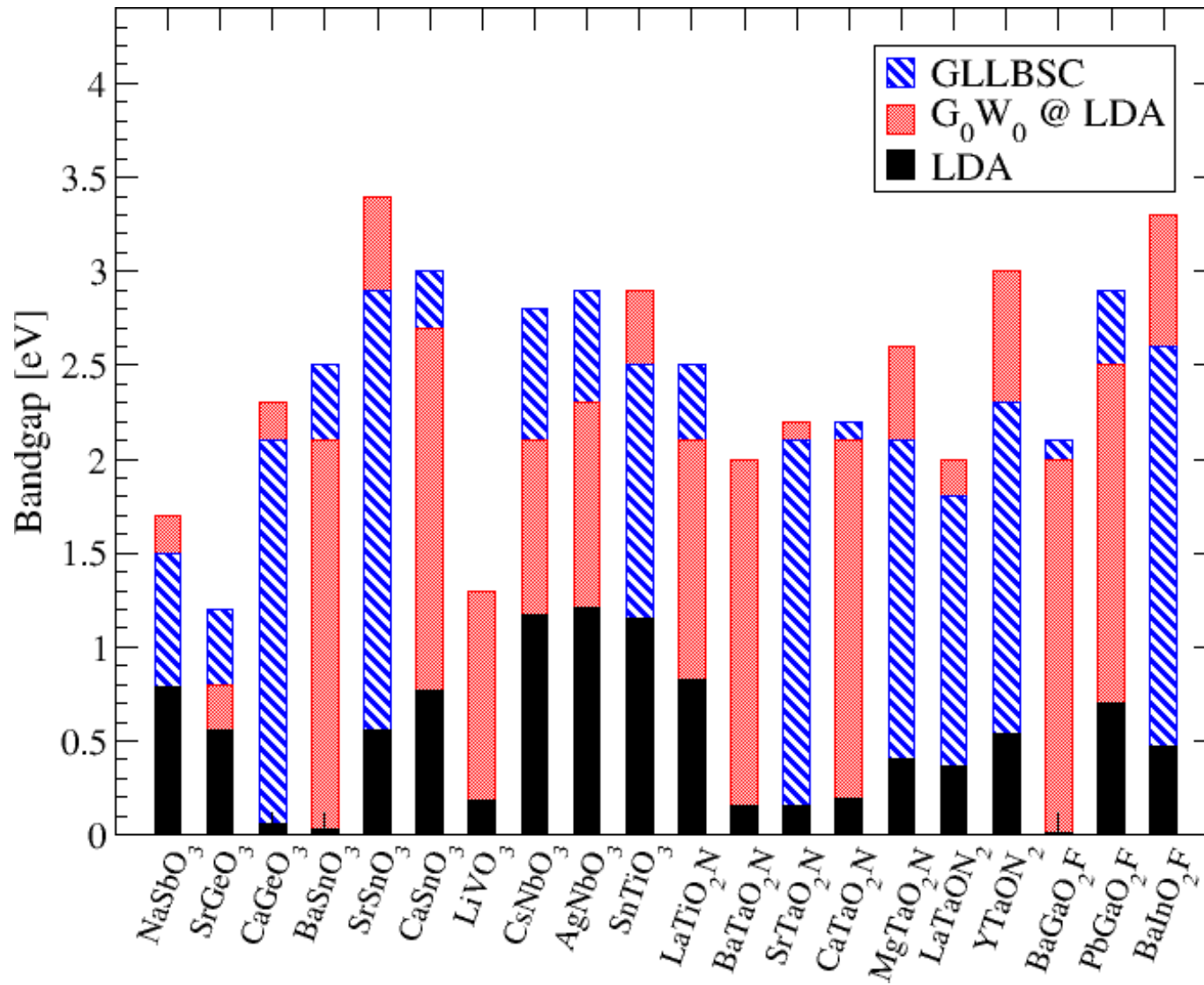
Chemical/structural stability (ΔE)
 Bandgap (E_{gap})
 Band edges
 (VB_{edge} , CB_{edge})

$\Delta E \leq 0.2 \text{ eV}$
 $1.5 \leq E_{\text{gap}} \leq 3 \text{ eV}$
 $\text{VB}_{\text{edge}} > 1.23 \text{ eV}$
 $\text{CB}_{\text{edge}} < 0 \text{ eV}$

- ABO_3 : 10 (AgNbO_3)
- ABO_2N : 5 (BaTaO_2N , SrTaO_2N , CaTaO_2N , LaTiO_2N)
- ABON_2 : 2 (LaTaON_2)
- ABO_2F : 3

I. E. Castelli, D. D. Landis, K. S. Thygesen, S. Dahl, I. Chorkendorff, T. F. Jaramillo, and K. W. Jacobsen, *Energy & Environmental Science*, **5**, 9034 (2012).

GLLB-SC and $G_0W_0@LDA$



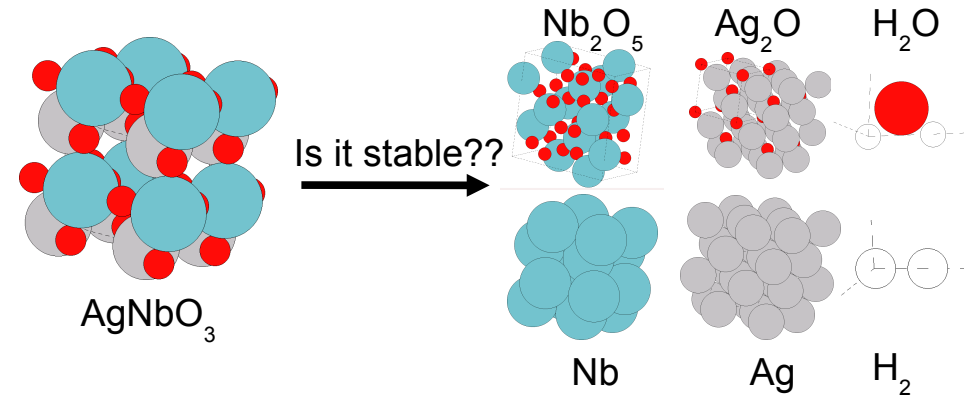
Good agreement between GLLB-SC and $G_0W_0@LDA$ within the plasmon-pole approx.

MAE = 0.345

Pourbaix Diagrams

Evaluation of the stability

So far: stability w.r.t. solid substances.



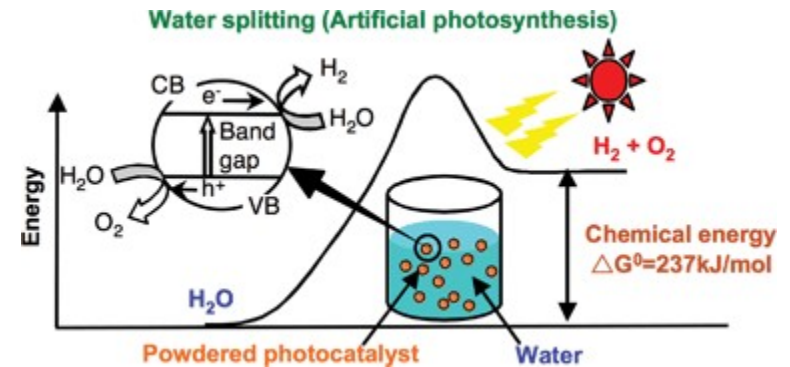
In a photocatalytic cell, the light harvester material is in touch with water.



Are our candidates stable also in water?

Evaluate the stability also w.r.t. dissolved substances and at various pH/potential.

→ **Pourbaix diagram**



Pourbaix Diagram for Zinc

General reaction:
 $rR + wH_2O = pP + hH^+ + ne^-$

Nernst equation at room temperature:

$$nE = \Delta G + 0.0591 \log \frac{(a_P)^p}{(a_R)^r} - 0.0591h \text{ pH}$$

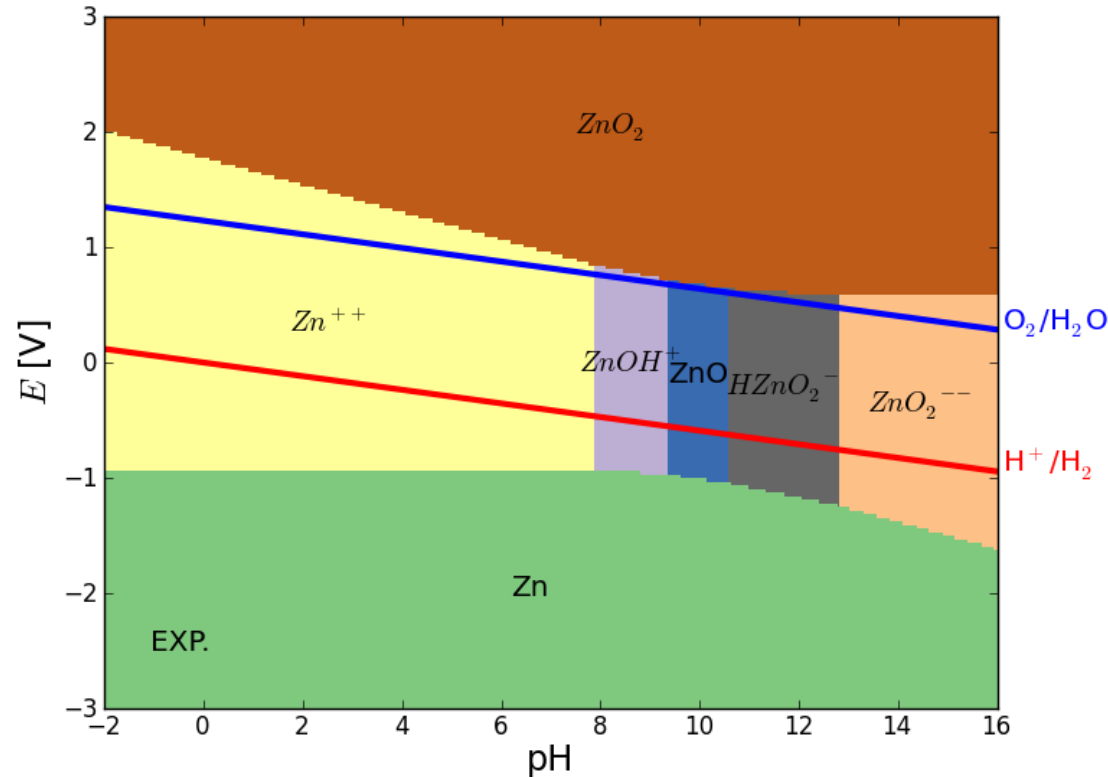
Solids: DFT

Dissolved substances:

Experiments

Three different lines:

- vertical: solid, dissolved substances and hydrogen ions. $ZnOH^+_{(aq)} = ZnO + H^+$
- horizontal: solid, dissolved substances with free electrons. $Zn^{++}_{(aq)} = Zn + 2e^-$
- straight with a slope equal to $0.0591h/n$: solid and dissolved substances with free electrons and hydrogen ions. $Zn + H_2O = ZnO + 2H^+ + 2e^-$



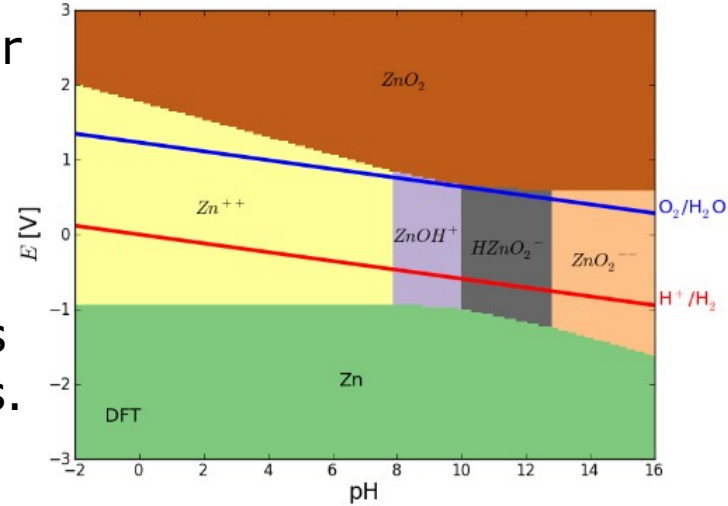
DFT vs Experiments

Pourbaix diagrams for Zn and Ti.

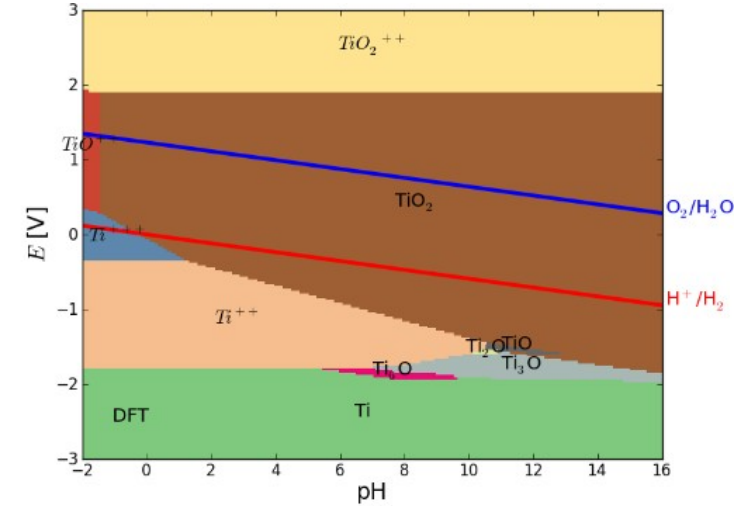
DFT and Experiments give similar diagrams.

Differences:

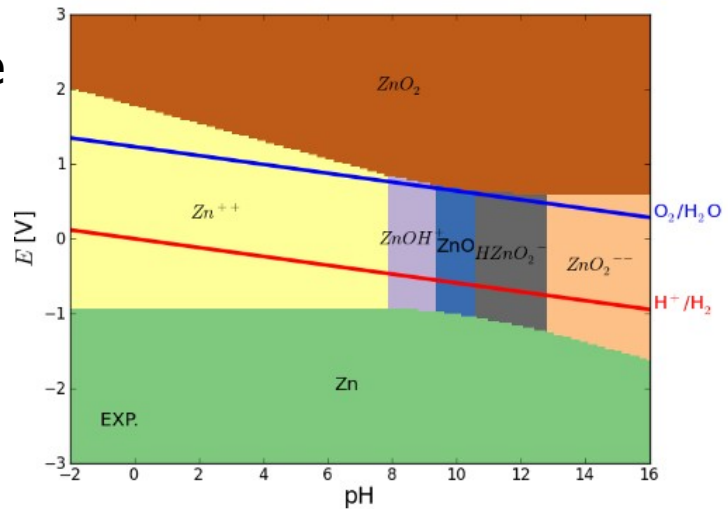
- inaccuracy in the data;
- more data available for DFT calculations.



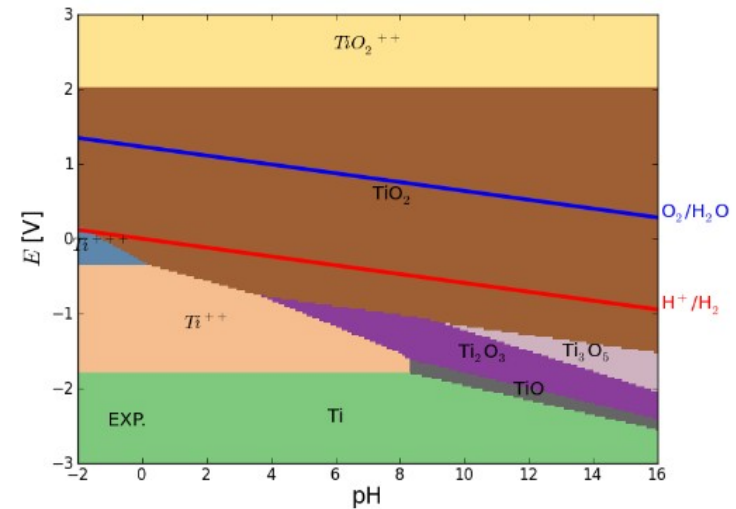
(a) ZnO - DFT



(b) TiO₂ - DFT

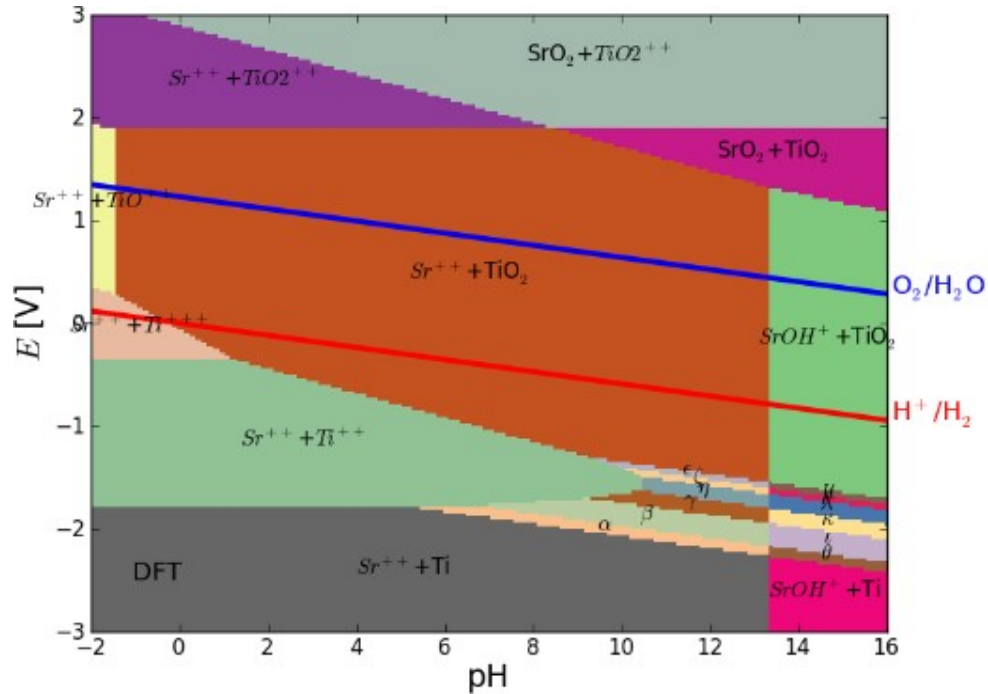


(c) ZnO - Experiments

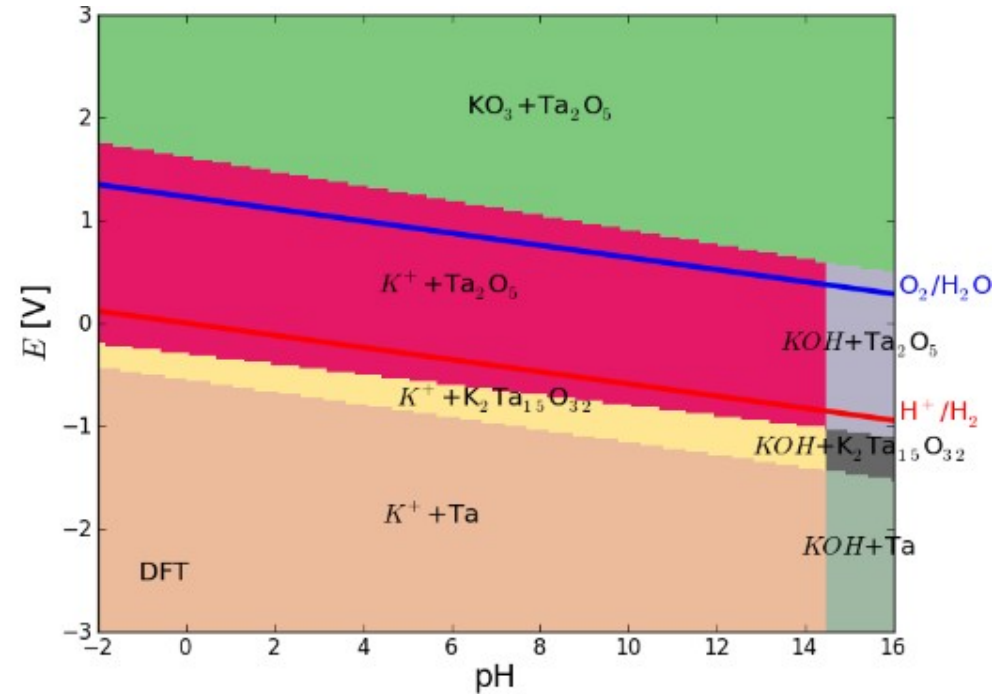


(d) TiO₂ - Experiments

SrTiO₃ and KTaO₃



(a) SrTiO₃ - DFT



(b) KTaO₃ - DFT

The cubic perovskite phase is **never** the most stable phase ($\Delta E < 0 \text{ eV/atom}$).

But they are experimentally known to be stable.

The reaction kinetics (not included in the Pourbaix diagrams) is important to find stable materials!

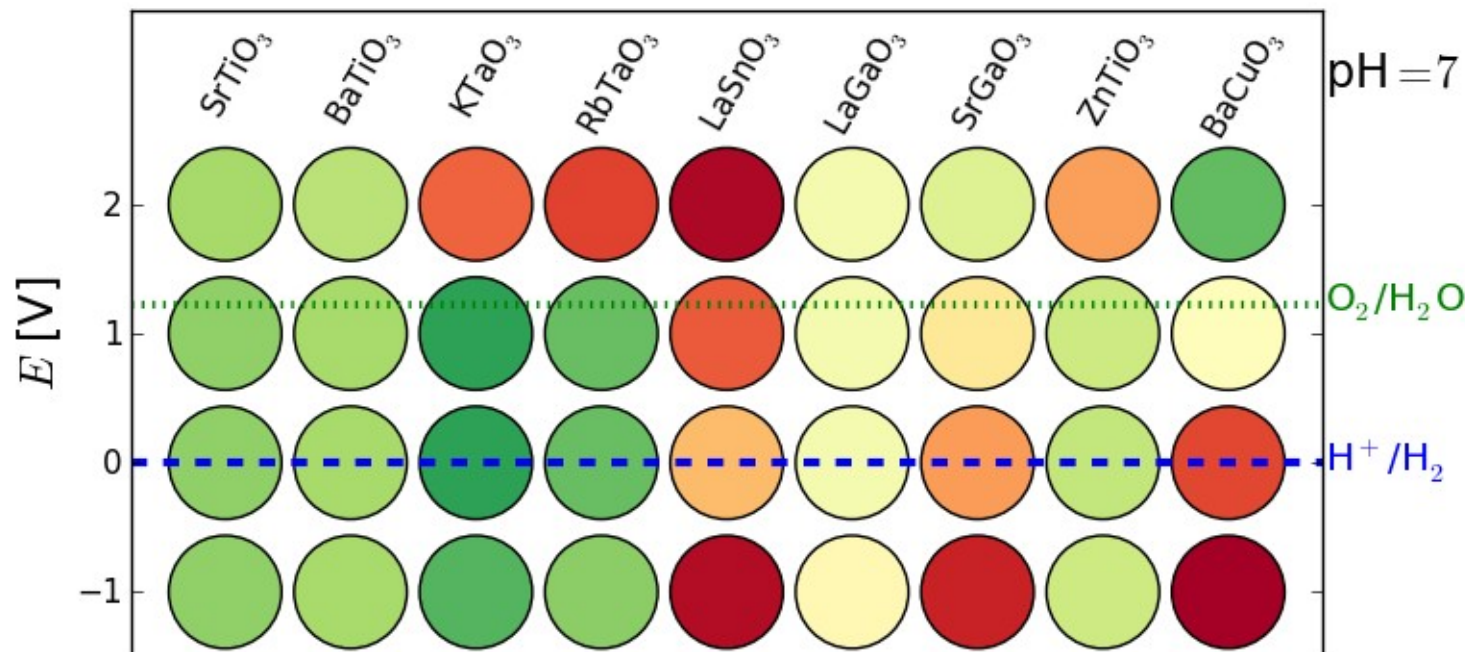
We can increase the energy threshold to take into account the kinetic term.

Stability of Known Perovskites

Stability analysis of selected cubic perovskites at pH=7 and potential equal to -1, 0, 1, and 2 V.

Only KTaO_3 is stable with a threshold of 0.2 eV/atom.

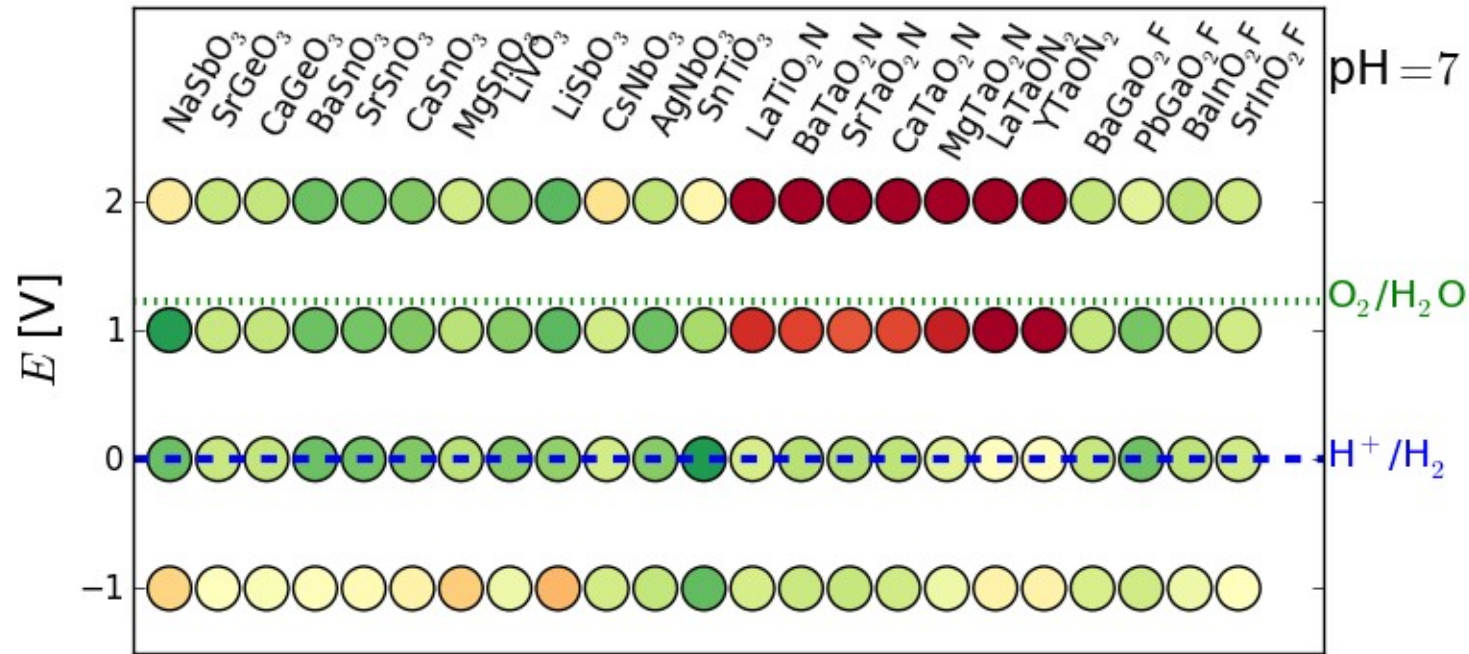
Few more are stable for a larger threshold (0.5 eV/atom).



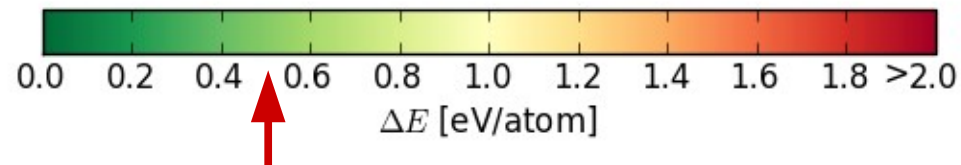
Water Splitting Candidates

Oxides and oxyfluorides have a region where they are stable ($\Delta E < 0.5 \text{ eV/atom}$).

Oxynitrides are less stable, especially at high potential.

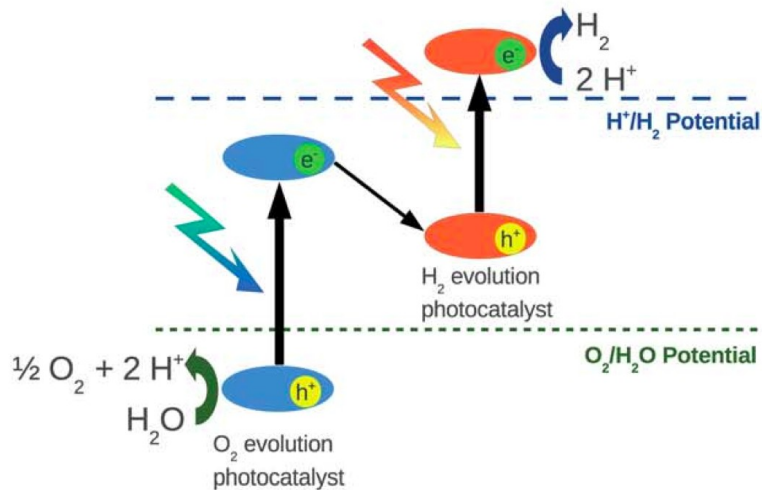


I. E. Castelli, K. S. Thygesen, and K. W. Jacobsen, *Submitted* (2013).



New stability threshold to account some metastability, inaccuracy in the calculations, and kinetic of the reactions.

Two-photon WS



Two semiconductors – two photons

- SC 1: Hole for oxygen evolution
- SC 2: Electron for hydrogen evolution

H_2 photocatalyst: Si

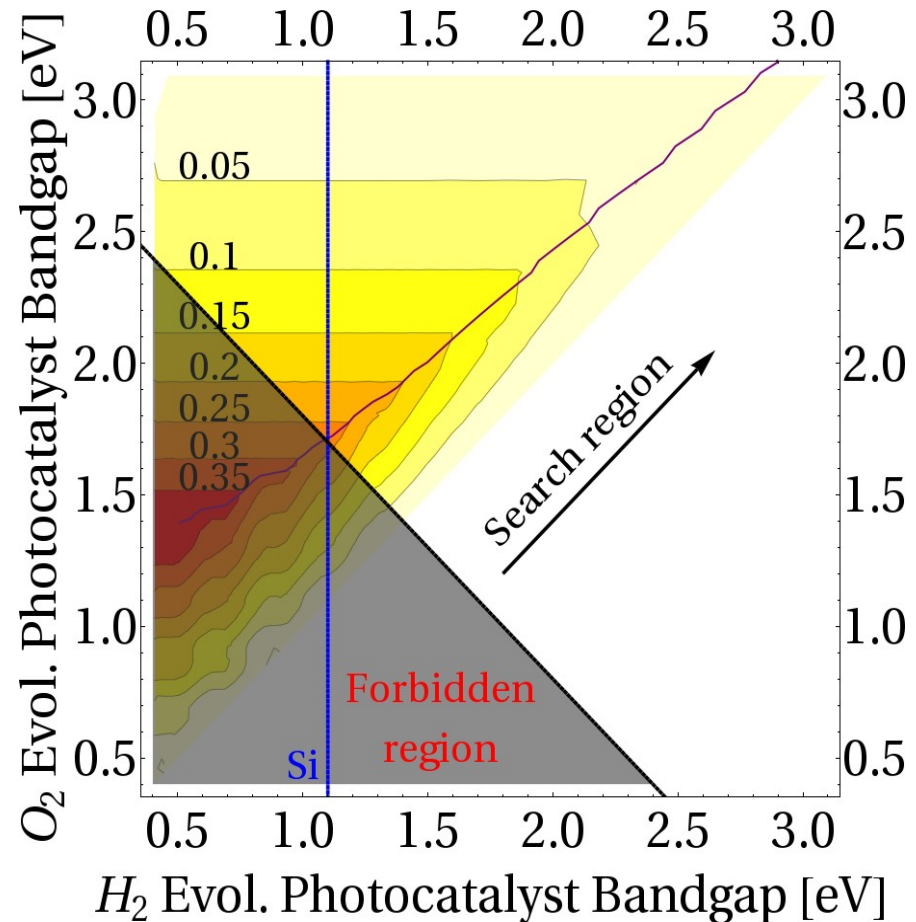
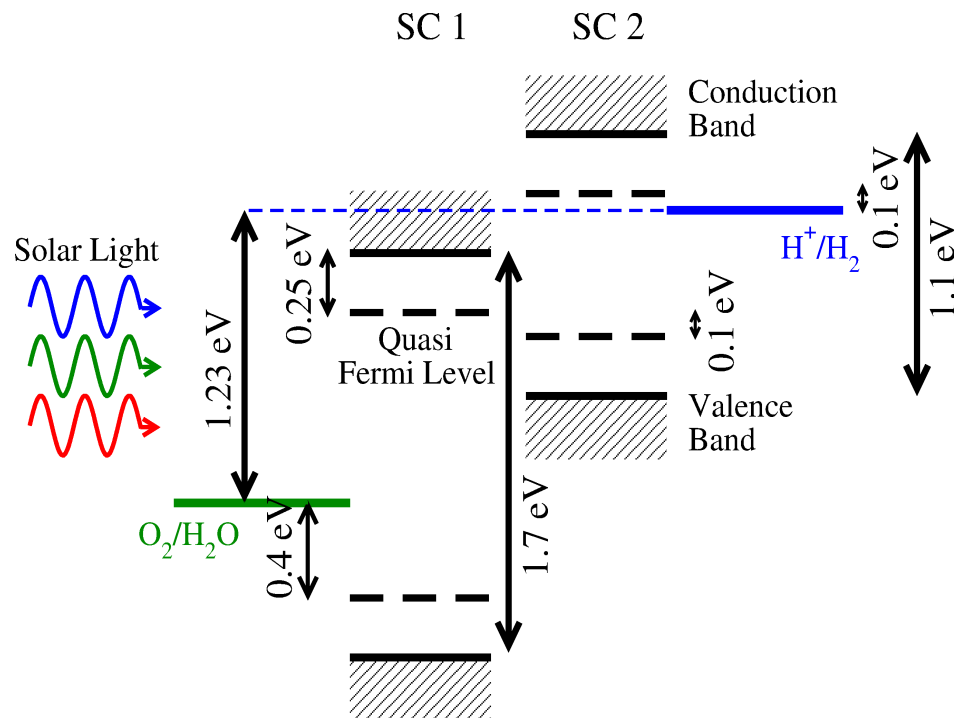
O_2 photocatalyst: screening

Requirements:

- structural/chemical stability;
- two visible light harvesters (optimal gaps: 1.1 eV and 1.7 eV);
- band edges that match with oxygen and hydrogen potentials;
- Small overlap between the semiconductors band edges for the electron transfer reaction.

Tandem Cell Efficiency

Solar-to-hydrogen energy conversion efficiency

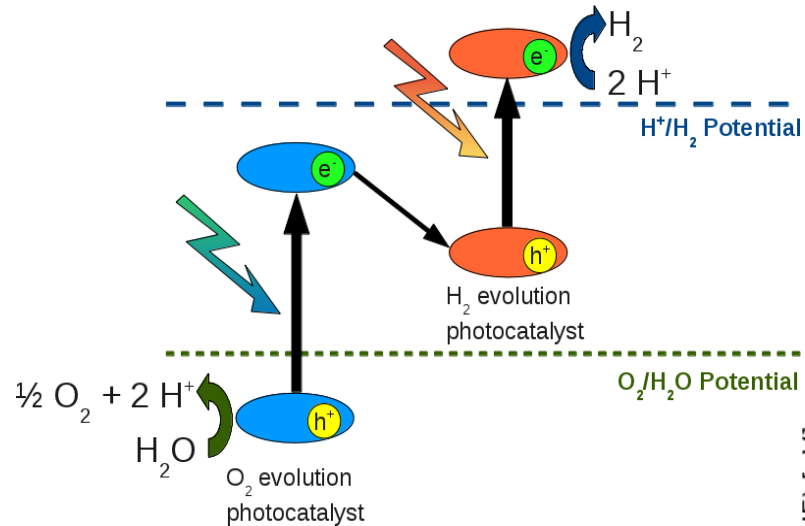


J. R. Bolton et al., *Nature* 1985.

M. G. Walter et al., *Chem Rev* **110**, 6446, 2010.

I. E. Castelli et al., *Energy & Environmental Science*, **5**, 9034 (2012).

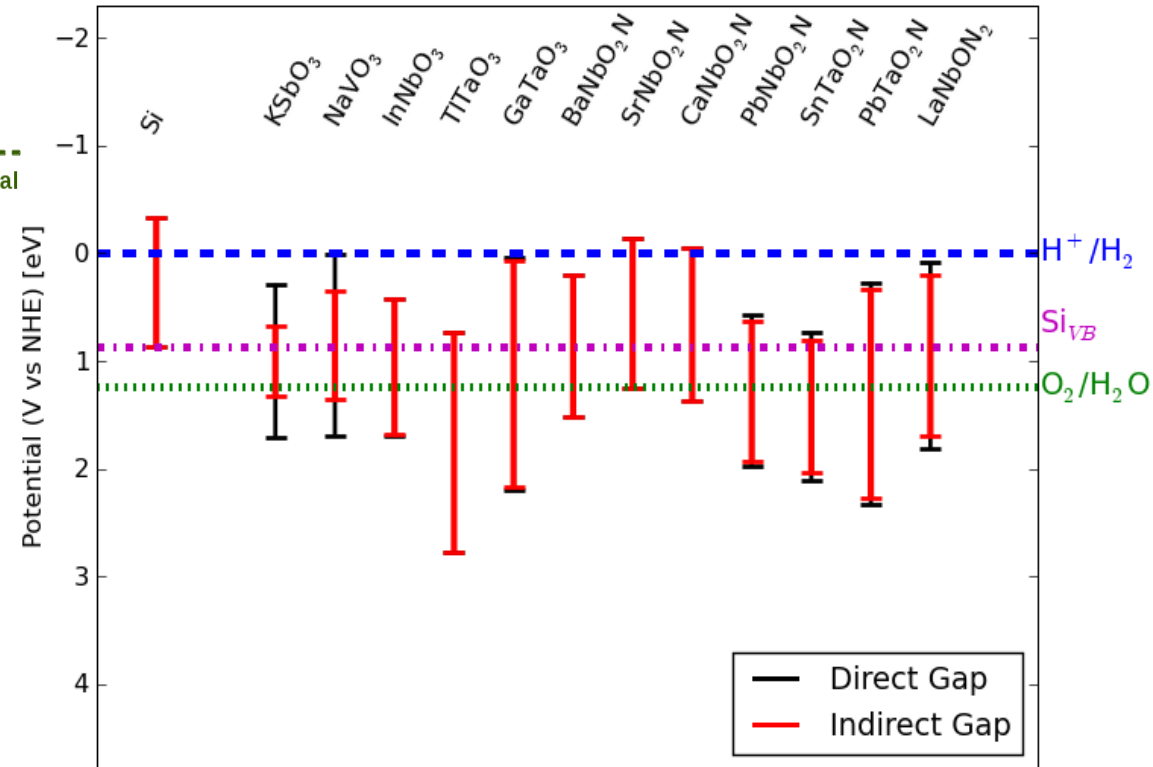
Two-photon WS: Candidates



$E_{\text{form}} < 0.2$

$1.3 < E_{\text{gap}} < 3 \text{ eV}$

12 candidates
+ 20 from overall WS



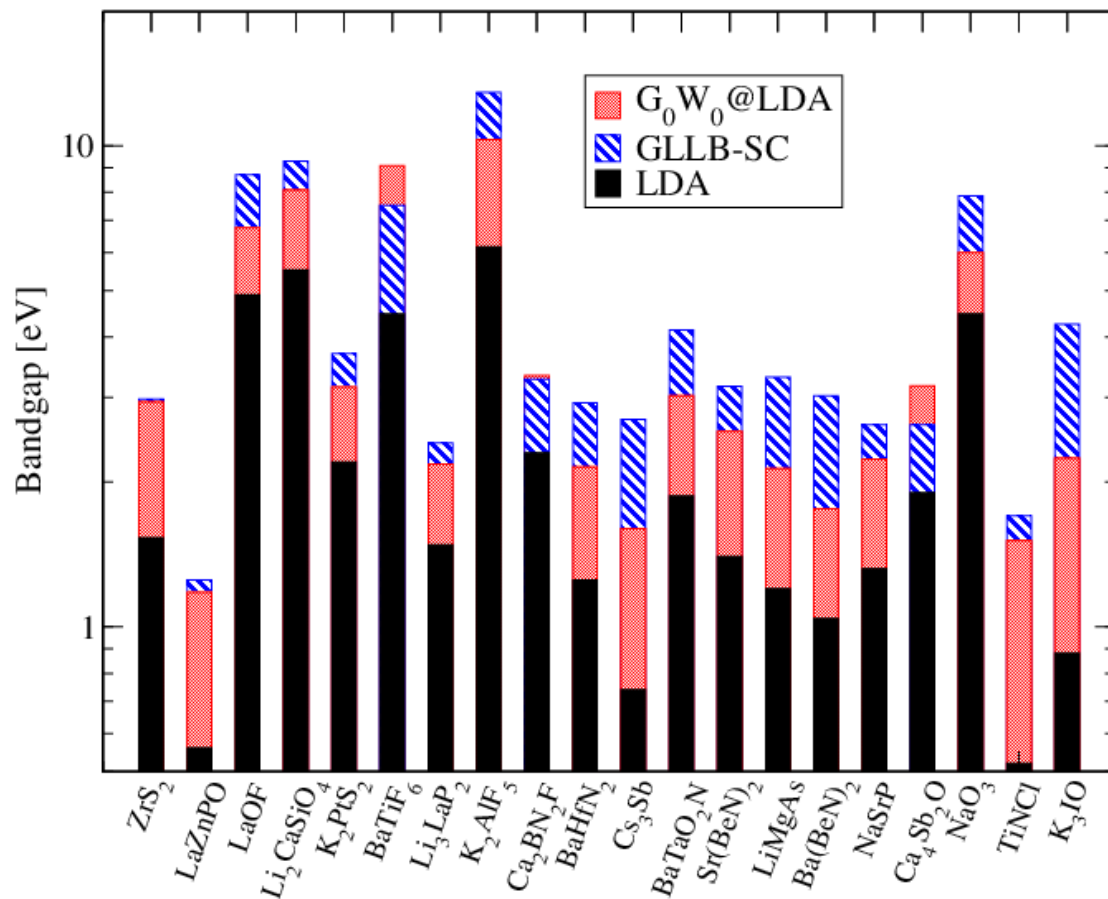
Materials Project Database

MATERIALS PROJECT

A Materials Genome Approach

Calculation of the bandgaps of 6000 known structures from the Materials Project database.

(in collaboration with: A. Jain and K. Persson, LBNL; G. Ceder, MIT).



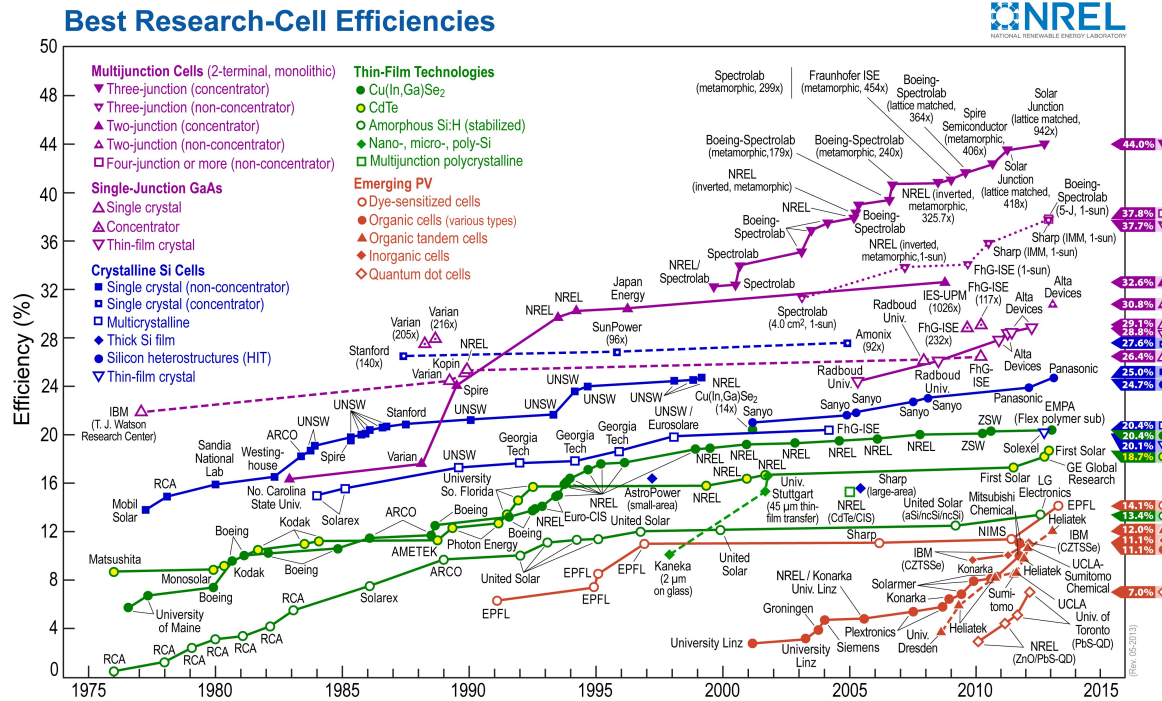
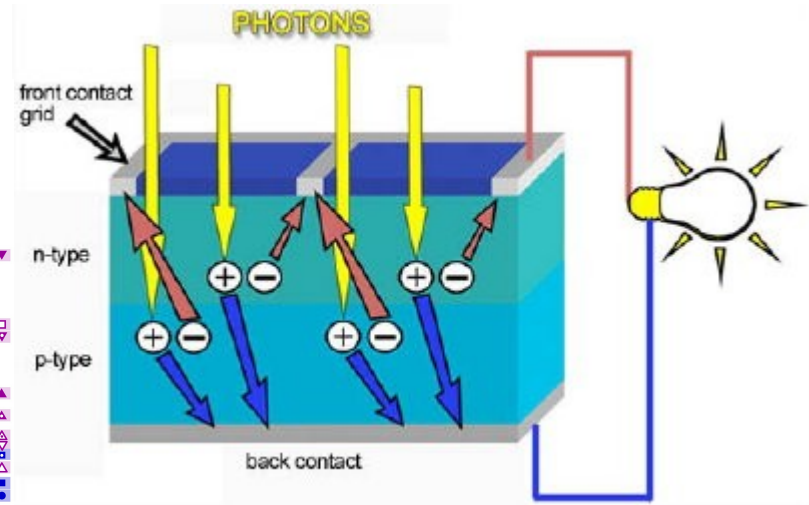
Reasonable agreement between GLLB-SC and G_0W_0 .

(Calculations from Falco Huser).

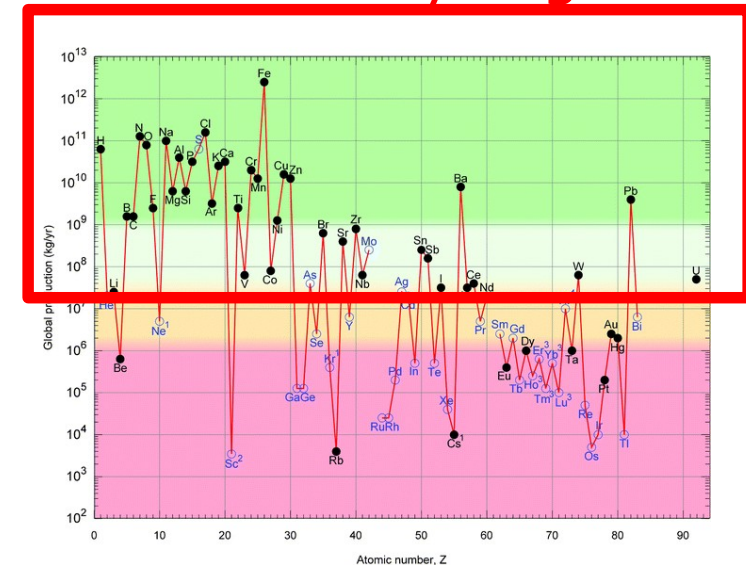
Applications: water splitting; photovoltaics; ...

Thin Film Solar Cell

Photons are used to create current.



Eco-friendly region

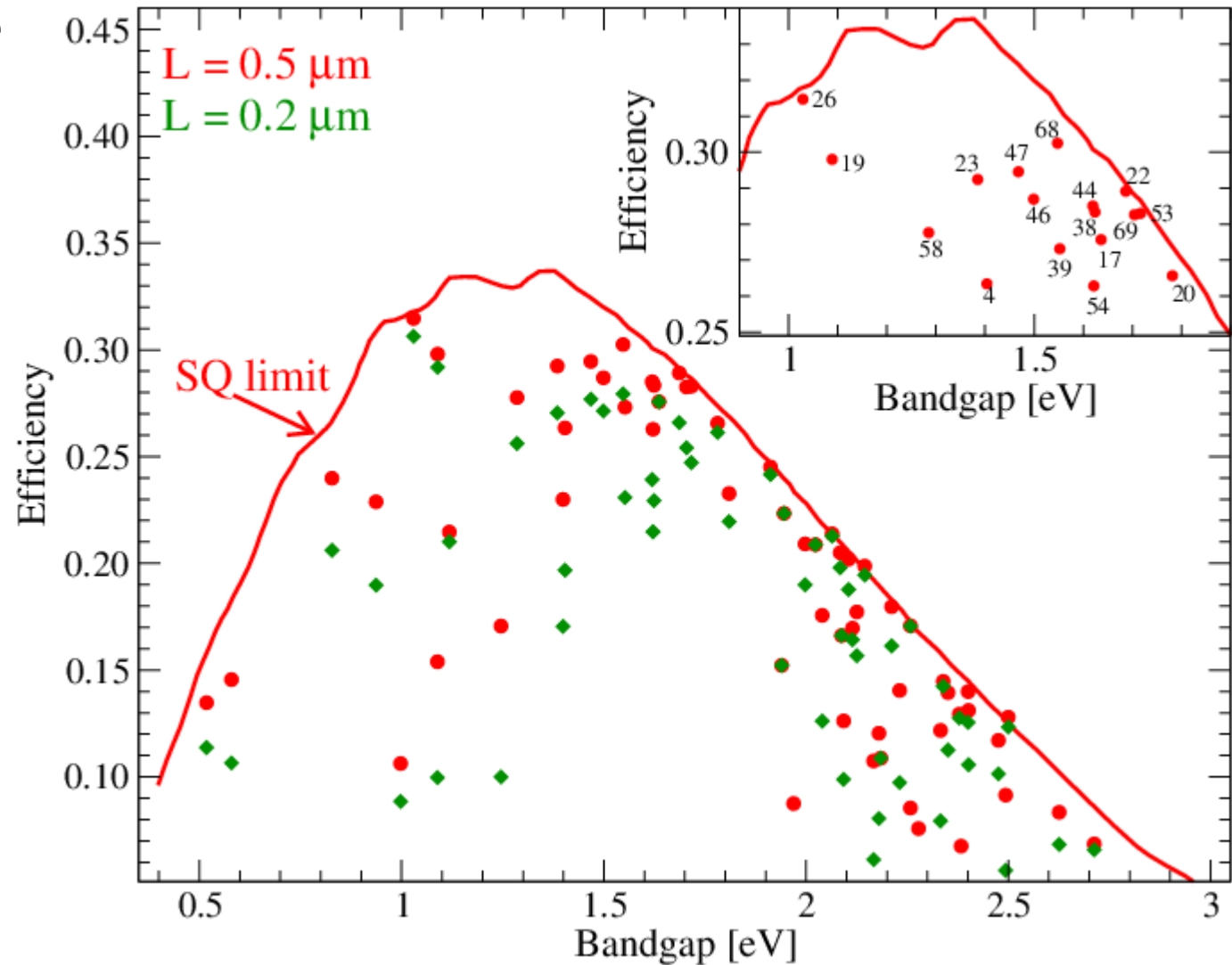


Calculation of the absorption spectra of 70 interesting known materials to use in a thin film SC.

Single-layer Thin Film SC

17 materials have a theoretical efficiency larger than 25 %.

4 have been already used in a SC.



Computational Materials Repository

[Hide search box](#)

[Link to image](#)

Do not forget to press **update matrix** after changing the selection!
If there is an error - it means that the dataset is already being calculated! Please wait a moments and try again.

Chose a data set: ABO3 (2704)

Width: 800

Height: 1200

X axis ticks: B

Y axis ticks: automatically selected

X sort order: Electronegativity (Paulin)

Y sort order: Electronegativity (Paulin)

Action on Click: show band edges

- References:
- ABN (3)
 - ABO (20)
 - AN (50)
 - AO (52)
 - AON (35)
 - default (3)
 - mbulk (52)

	Value field:	Colors:
Triangle 1: (top-right)	gllbsc_ind-gap (eV)	0->white,0.7->purple,2.2->red
Triangle 2: (bottom-left)	heat_of_formation (eV)	min->red,0.3->white,4->blue
Triangle 3:		
Triangle 4:		

Examples for the color choice:

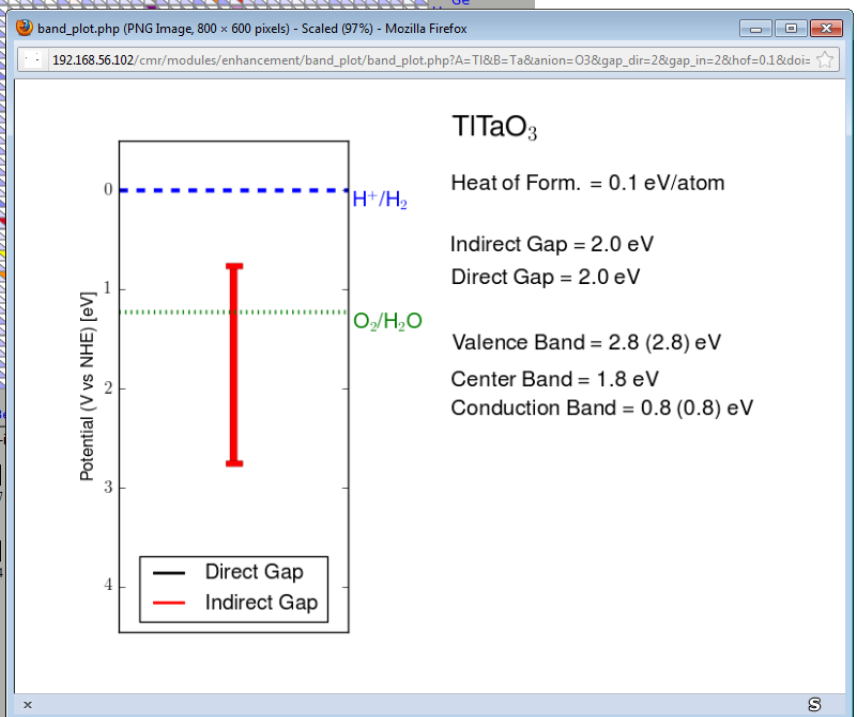
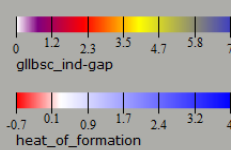
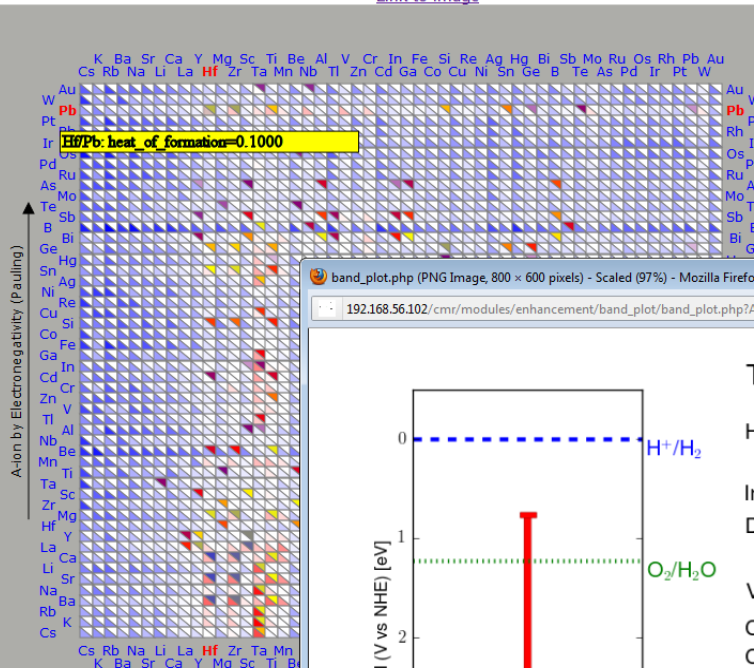
0->white,1->red,7->blue

0->white,0.9->red,2.2->green,4->yellow,8->blue

-100->blue,100->red

Valid color names are black, blue, cyan, green, gray, green, lightblue, pink, red, purple, white, yellow. Please note that the values must be in **increasing** order.

Update matrix



<http://cmr.fysik.dtu.dk> - the database

<http://wiki.fysik.dtu.dk/cmr> - the software

Conclusions

- Few materials (40) have been identified for one- and two-photon water splitting;
- The GLLB-SC potential works well for bandgap calculations;
- 17 materials have been proposed for single-layer thin film solar cell;
- A database has been developed for an easy access to the data.

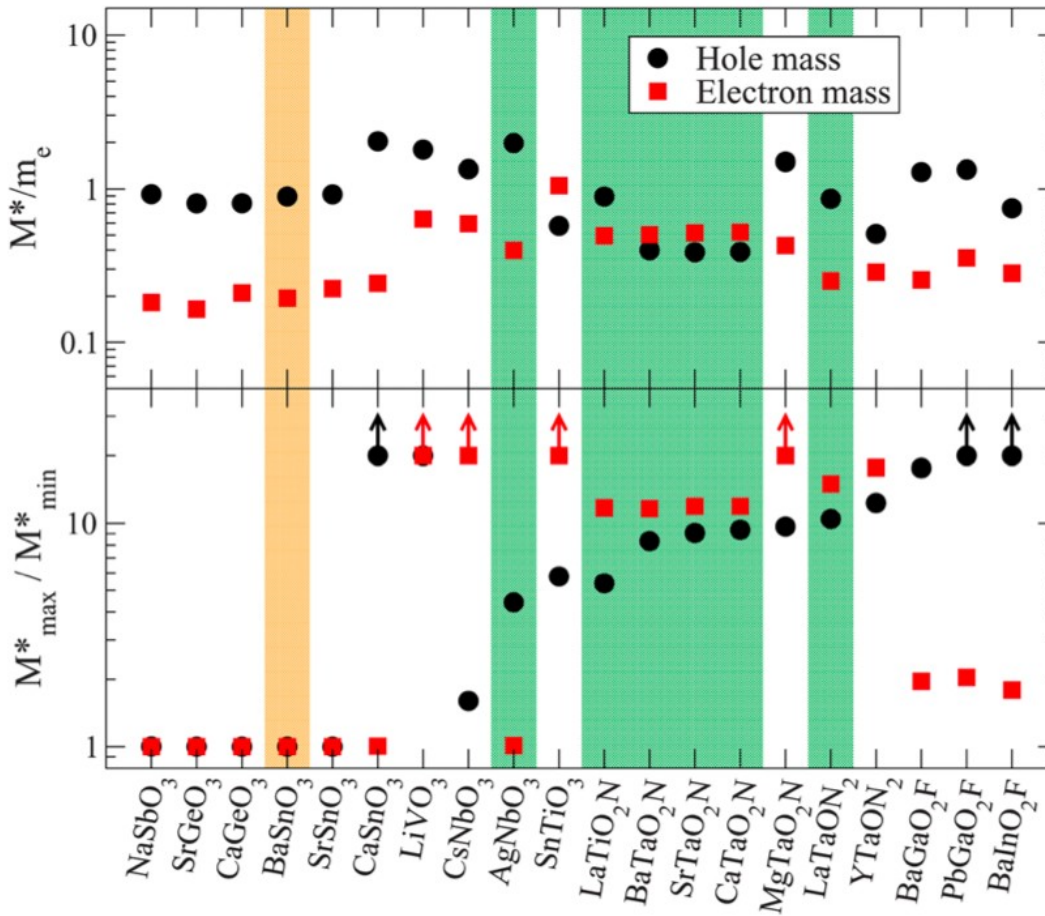
Acknowledgment

Karsten W. Jacobsen
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David D. Landis
Thomas Olsen
Falco Huser

CAMd
Center for Atomic-scale Materials Design

CASE
Catalysis for Sustainable Energy

e-h Masses and Mobility



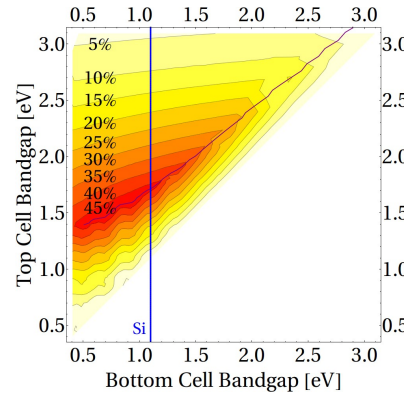
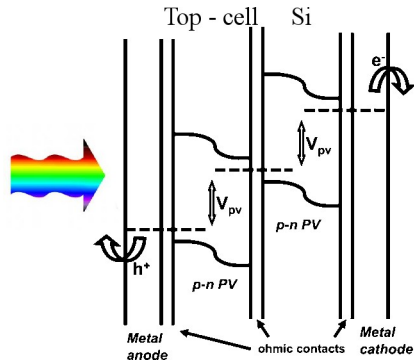
$$\frac{1}{M^*} = \frac{1}{3} \left(\frac{1}{m_x^*} + \frac{1}{m_y^*} + \frac{1}{m_z^*} \right)$$

Green systems: known to split water (with sacrificial reagents).

Orange system: BaSnO₃ known not to work (probably defect-assisted recombination).

Systems observed to work seems fairly isotropic.

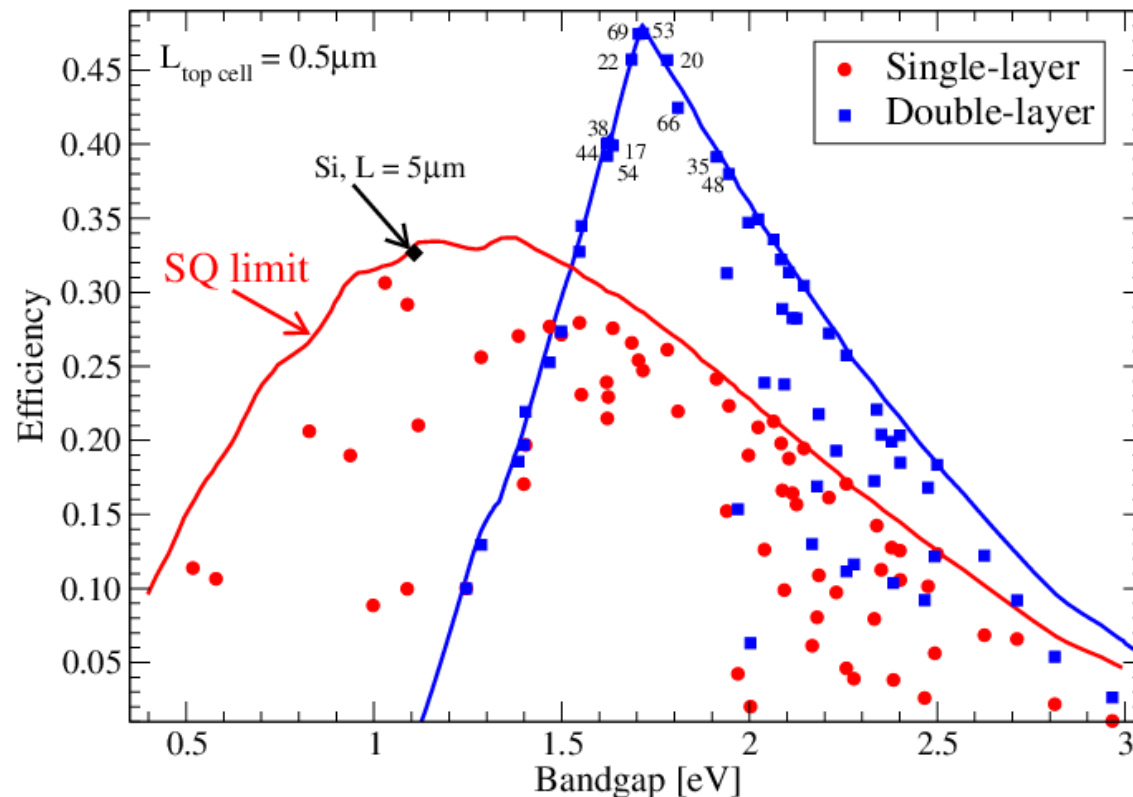
Double-layer Thin Film SC



Top-cell: ???
Bottom-cell: silicon

11 materials have an efficiency of more than 35 %.

3 of them have been used so far in a SC.



Background

Design